UNIT 1: NON-CALCULATOR, HIGHER TIER GENERAL INSTRUCTIONS for MARKING GCSE Mathematics - Numeracy

- 1. The mark scheme should be applied precisely and no departure made from it. Marks should be awarded directly as indicated and no further subdivision made.
- 2. <u>Marking Abbreviations</u>

The following may be used in marking schemes or in the marking of scripts to indicate reasons for the marks awarded.

cao = correct answer only

MR = misread

PA = premature approximation

- bod = benefit of doubt
- oe = or equivalent

si = seen or implied

ISW = ignore subsequent working

F.T. = follow through (\checkmark indicates correct working following an error and \checkmark indicates a further error has been made)

Anything given in brackets in the marking scheme is expected but, not required, to gain credit.

3. <u>Premature Approximation</u>

A candidate who approximates prematurely and then proceeds correctly to a final answer loses 1 mark as directed by the Principal Examiner.

4. <u>Misreads</u>

When the <u>data</u> of a question is misread in such a way as not to alter the aim or difficulty of a question, follow through the working and allot marks for the candidates' answers as on the scheme using the new data.

This is only applicable if a wrong value, is used consistently throughout a solution; if the correct value appears anywhere, the solution is not classed as MR (but may, of course, still earn other marks).

- 5. <u>Marking codes</u>
 - 'M' marks are awarded for any correct method applied to appropriate working, even though a numerical error may be involved. Once earned they cannot be lost.
 - 'm' marks are dependant method marks. They are only given if the relevant previous 'M' mark has been earned.
 - 'A' marks are given for a numerically correct stage, for a correct result or for an answer lying within a specified range. They are only given if the relevant M/m mark has been earned either explicitly or by inference from the correct answer.
 - 'B' marks are independent of method and are usually awarded for an accurate result or statement.
 - 'S' marks are awarded for strategy
 - 'E' marks are awarded for explanation
 - 'U' marks are awarded for units
 - 'P' marks are awarded for plotting points
 - 'C' marks are awarded for drawing curves

UNIT 1: NON-CALCULATOR, HIGHER TIER

GCSE Mathematics – Numeracy	Mark	Comment
1. Perpendicular bisector Stornaway and Ullapool	B1	
(±2°) Use of correct scale (1cm = 10 miles)	B1	Award for use of 3cm in arc or 1cm in free
Arc from Portree 30 miles shown as	B1	hand drawing below
approximately 3× distance Muir to Dingwell (i.e.		
3cm) Free hand distance 10 miles off shore (i.e. 1cm)	B1	FT their Muir to Dingwall distance
Indication of possible sightings	B1	FT for attempted perpendicular and arc
Range of bearing ±2°	B2	only FT provided at least B2 previously
		awarded
		range
2 (a) Area of and 10.11 ± 10.2	7	
Area of the floor: 20.1×10	B1	
Vertical sides with slopes: $\frac{1}{2} \times 20 \times (1+3) \times 2$	B1 M1	May be seen with a calculation x£25
$10x1 + 10x3 + 20.1x10 + 2 x\frac{1}{2}x20x(1+3)$		previously awarded.
(10 + 30 + 201 + 80 or 10 + 30 + 201 + 40 + 40=)		
321 (m²)	A2	A1 for at least 3 areas accurately evaluated in a sum of areas of 5 sides
Total cost £ 321 × 20 + 6 × 150	M1	FT 'their derived 321'
(£)7320	A1	
$2(b)(i) > \pounds 140$: with pool 120 – 105 (=15) AND	M1	
10 (hotels)	A1	
(ii)		
Median (£) IQR (£)	B3	Medians and IQRs correct
With pool 108 $(130 - 74 =)$		B2 for any 3 of the 4 correct B1 for any 1 or 2 of the 4 correct
Without pool 74 (90 - 66 =)		,
Interpretation must refer to the greater spread	E1	Depends on previous award of at least B2
or equivalent e.g. The prices are generally lower		
and less varied in hotels without pools.	14	
3.(a) £1 coin	B1	
(b) 8×10 ⁻³ (c) 307	B1 B1	
(d) 3860 ÷ 200	M2	M1 for digits 3860 divided by 200 with
19.3 (a/cm ³)	A1	incorrect place value
	6	
4.4 × $\frac{1}{3}$ or equivalent × 2½ or equivalent.	M1 M1	
= 20/6(hrs) or equivalent OR 200(min)	A1	Do not accept 20 ÷ 6.
= 3nrs 20 min.	A1	difficulty.
		If question is misread as 'It took Machine A d hours How long did it take
		Machine B?
		Award SC1 for $(4 \times 3) / 2\frac{1}{2}$ or 4.8 hours and a further SC1 for 4hrs 48min
	4	

GCSE Mathematics – Numeracy	Mark	Comment
5.(a) ¼ or equivalent (b) TRUE FALSE TRUE TRUE	B1 B2	B1 for any 4 correct
FALSE	3	
6.(a)(i) (800 – 300)/ 50 = 10 (ii) Explanation, e.g. 'extra cost per person', '£10 per person', '£100 extra for every 10 people' (iii) Explanation, e.g. 'fixed charge' (b) (£)200	M1 A1 E1 E1 B1	Or equivalent Do not accept 'more people the more paid' FT from their gradient if reasonable Accept 'conference cost starts at £300', or 'hire cost' CAO
7.(a) Using ratio 30 : 1 or equivalent. (Ratio of areas =) 900 : 1 or equivalent. (Area of large logo =) 5×900 (= 4500 cm ²) (Cost =) (£)200 × 0.45 (£) 90 Organisation and communication Accuracy of writing	5 B1 M1 m1 A1 OC1 W1	Allow M1 for sight of 270 : 9 or equivalent notation. F.T. '(their length ratio) ² '.
(b)(i) Perimeter = $a - 5b + 2c - d$ (ii) Area = $a(5b + 2c - d)$	B1 B1 9	
8. (a) Tangent at t = 30 Use of difference in v / difference in t Acceleration (reasonable for their tangent) m/s^2 or ms^{-2}	M1 M1 A1 U1	Accept with or without sight of a tangent Must be evaluated from their tangent Independent
(b) Use of area under the curve from 0 to 30 seconds	S1	Treat area 0 to 50 seconds as MR-1 then FT
Correct method, including ½x4x30 or ½x5x30 Correct answer to calculation, e.g. 60(m) to 75(m)	M1 A1 7	Accept any suitable calculation for 1 or more blocks of area If units are given they must be correct <i>Trapezium rule (approximate values)</i> 10x[0+4.4+2(1.75+3.4)]/2 = 73.5(m)
9. (a)Frequency density = 1 indicated on graph	B2	B1 for sight of 1 or 2 ÷ 2
(b) FALSE TRUE FALSE FALSE FALSE	B2	B1 for 4 correct
(c) Total number of pupils: $5x^2 + 14x^{0.5} + 10x^{0.5} + 6x^{1} + 4x^{1} + 1x^{2}$ S to Z seconds total number:	M1 A1	(10 + 7 + 5 + 6 + 4 + 2)
$(14 \times 0.5 + 10 \times 0.5 + 6 \times 1 =)$ 18 Convincing 60% of 34 = 20.4 which is > 18 or 18 is 60% of 30, so it's less than 60% of 34.	B1 B1 8	FT provided at least 2 of the 3 correct FT provided similar difficulty Alternative method 18/34 ≈ 0.529 or 52.9% <60%

GCSE Mathematics – Numeracy Unit 1: Higher Tier	Mark	Comment
10. (£)120 × 1⋅2 (£)144 (£)144 ÷ 0⋅75 or equivalent (£)192	M1 A1 M1 A1 4	FT 'their (£)144'
11.(a) (i) ¾ × 28 × (£) 8 (million) × 1.1 (£) 184.8 million or equivalent (ii) £1 × 10 ⁸	M1 m1 A1 B1	
(b)(i) M25 1/5 longer than M62 or equivalent	M1	Decide on reasonable comparison
e.g. (1960-1976) 7.7x10 ⁸ x6/5 (for approximately same length of M25) 9(.24) x10 ⁸	M1 A1	Method calculation (with approximations) for comparison Accurate calculation (with approximations)
Conclusion, e.g. 'very similar cost per mile'	E1	Accept a conclusion that there was a decrease in costs e.g. No, there was a decrease of about £33 000 per mile
(b)(ii) Decision, e.g. to estimate an average cost for a vehicle for the period, e.g. car £4, lorry £10	S1	
Reasonable accurate calculation for toll fees for 1 day, e.g. 20 000×4 + 19 000×10 = (£) 270 000 (per day)	B1	
Build cost ÷ toll fee taken per day (may include approximation) 900 000 000 ÷ 270 000 (≈ 3300) OR 900 000 000 ÷ 300 000 (=3000) ÷365	M1	OR Build cost ÷ toll fee taken per month
(or approximation of the days in a year, e.g. 300 or 350) $(3300\div365 \approx 9 \text{ years}) (3000\div300 = 10 \text{ years})$		
Accept answers between 8 to 11 years from reasonable approximations and accurate calculations (may be approximations) AND	A1	OR ÷12 (when working in months)
assumptions/approximations/estimates have been clear in working.		Additional assumptions may include that the costs given are able to be compared or that comparable effects of inflation are being overlooked etc.
	13	Additional method Daily revenue in 2003 = $20000 \times 2 + 19000 \times 10 = (\pounds)230000$ Number of days = $9 \times 10^8 \div 230000 \approx 4000$ days, i.e. about 11 years Daily revenue in 2012 = $20000 \times 5.5 + 19000 \times 11 = (\pounds)319000$ Number of days = $9 \times 10^8 \div 319000 \approx 3000$ days, i.e. about 8 years So, it will take between 8 years and 11 years to recover the costs, so about 10 years