

# REVISE

*.wales*

## 3.08 – Graphical solutions to quadratics

*Mark schemes for the 3.08 question pack*

*Spec 2.4.10 – Unit 3*

SOLUTIONS · 2025 SPECIFICATION

*Mark schemes for the 9 questions in the corresponding revise.wales question pack (18 marks total). Sources: legacy WJEC GCSE papers, WJEC SAM, and custom-authored mark schemes. Pack layout © revise.wales.*

2.(a)	6            -3		B2	B1 for each.
2.(b)	7 correct plots. Curve drawn.		P1 C1	<u>Use overlay.</u> F.T. 'their (-1,6)' and 'their (2,-3)'. Allow $\pm$ '½ a small square'. F.T. 'their plots'. At least 6 plots required. Clear intention to draw a curve through 'their plotted points'.
2.(c)	-0.9    and    3.4		B2	B1 for each. Allow (-0.9, 5) and (3.4, 5). F.T. intersection of 'their curve' with $y = 5$ provided exactly 2 intersections seen on graph. Allow $\pm$ '½ a small square'.  <u>If no marks gained</u> then SC1 for either of the following. $y = 5$ drawn correctly, OR <u>Two</u> correct F.T. values given for 'their straight line' and 'their curve' provided exactly 2 intersections seen on graph.
2.(d)	$2x^2 - 5x - 6 = 0$		B1	

1320	ISW		
18. Sight of (0), 1, 4, 9, 16, 25 and 36. Split into 6 areas AND attempt to add derived areas  Correct substitution into trapezium rule. Area = $\frac{1}{2} [0 + 36 + 2(1 + 4 + 9 + 16 + 25)]$  - 72	✓ ✓  ✓  ✓	B1 M1  M1  A1	Penalise -1 once only for a <u>consistent</u> misreading of one scale.  If using 6 separate areas, at least one area calculation (for a trapezium) should be potentially correct. 1st M1 may be implied by correct use of formula. Or equivalent (0·5+2·5+6·5+12·5+20·5+30·5) F.T. 'their values of y' provided at least 2 correct. Allow 1 slip e.g. in a y-value term, in h, or in an individual area.

1.(c)	knombus	B1	
2.(a)	-3	B1	
	Scale on y-axis '2cm square $\equiv$ 5 units' OR '2cm square $\equiv$ 4 units'.	B1	B0 for '2cm square $\equiv$ 10 units'.
	At least 5 correct plots and no incorrect plot.	P1	F.T. 'their (-1, -3)' AND 'their uniform scale' if possible. Allow $\pm$ '½ a small square'.
	A smooth <u>curve</u> drawn through their plots.	C1	F.T. 'their 6 plots' OR a curve through the 5 given plots and (-1, -3). Allow for the intention to pass through their plots. ( $\pm$ 1 small square horizontal OR vertical).
2.(b)	$y = x^2 + 3$	B1	

16)

Graph A

$y = 7x^2$	
$y = -(x + 7)^2$	
$y = (x - 7)^2$	
$y = 7 - x^2$	✓
$y = x^2 + 7$	

B1

Graph B

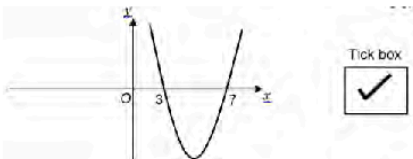
$y = x^2 + 1$	
$y = 2^x$	✓
$y + 1 = x^2$	
$y = \frac{1}{x}$	
$v = r^o$	

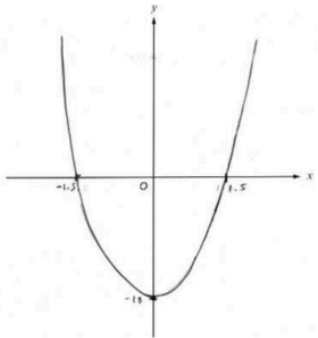
B1

18. Translation horizontally to the right (only) (4, 2) indicated correctly.	B1 B1	Minimum point at (4, 2). SC1 for left shift with (-4, 2) indicated.
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<p>15.</p> <p>Graph</p> <p>Equation</p> <p><math>y = (x + 1)(x - 4)</math></p> <p><math>y = (x - 4)^2</math></p> <p><math>y = x(x + 4)</math></p> <p><math>y = (x - 1)(x + 4)</math></p> <p><math>y = (x - 2)(x + 2)</math></p> <p><math>y = x(x - 4)</math></p> <p><math>y = (x + 1)(4 - x)</math></p> <p><math>y = (1 - x)(x + 4)</math></p> <p><math>y = (x + 4)^2</math></p>	<p>B2</p>	<p>B1 for any 1 or 2 correct.</p>
<p>16.(a) General sine curve with appropriate orientation and position.</p> <p>-1 and 1 indicated on the y-axis, curve passes through <math>(-180^\circ, 0)</math>, <math>(0^\circ, 0)</math> and <math>(180^\circ, 0)</math> and approximately <math>(-90^\circ, -1)</math> and <math>(90^\circ, 1)</math>.</p>	<p>M1</p> <p>A1</p>	<p>Ignore curve shown for values <math>x &lt; -180^\circ</math> or <math>x &gt; 180^\circ</math>.</p>
<p>16(b). <math>-30^\circ</math> AND <math>-150^\circ</math></p>	<p>B2</p>	<p>Accept embedded answers. Penalise further incorrect answer(s) -1. Ignore further answer(s) outside of the range.  Award B1 for sight of an answer <math>-30^\circ</math> or <math>-150^\circ</math> (but not for sight of <math>-30</math> as part of working).</p>
<p>17.(a)</p> $\frac{3}{100} \times \frac{1}{99}$ $= \frac{3}{9900} \left( = \frac{1}{3300} \right) \text{ ISW}$	<p>M1</p> <p>A1</p>	<p>Allow <math>3(.03\dots) \times 10^{-4}</math> OR <math>0.0003(03\dots)</math> or equivalent. A0 for <math>0.0003(03\dots)\%</math>. An unsupported <math>0.000303(\dots)</math> gains M1A1. An unsupported <math>3/10000</math> OR <math>0.0003</math> gains no marks.</p>
<p>17(b)</p> $2 \times \frac{3}{100} \times \frac{1}{99} \left( = \frac{6}{9900} = \frac{1}{1650} \right)$ $+ \frac{3}{100} \times \frac{2}{99} \left( = \frac{6}{9900} = \frac{1}{1650} \right)$ <p>OR</p> $\frac{4}{100} \times \frac{3}{99}$ $= \frac{12}{9900} \left( = \frac{1}{825} \right) \text{ ISW}$	<p>M2</p> <p>A1</p>	<p>M1 for sight of <math>\left( \frac{3}{100} \times \frac{1}{99} \right) + \left( \frac{3}{100} \times \frac{1}{99} \right)</math> OR <math>\left( \frac{3}{100} \times \frac{1}{99} \right) + \left( \frac{1}{100} \times \frac{3}{99} \right)</math> OR <math>2 \times \frac{3}{100} \times \frac{1}{99}</math> OR <math>\left( \frac{3}{100} \times \frac{1}{99} \right) + \left( \frac{3}{100} \times \frac{2}{99} \right)</math></p> <p>A1 Allow <math>1(.21\dots) \times 10^{-3}</math> OR <math>0.001(21\dots)</math> or equivalent. An unsupported answer of <math>0.00121(2\dots)</math> gains M2A1. A0 for <math>0.001(21\dots)\%</math>. SC1 for working with replacement leading to an answer of <math>12/10000</math> (<math>3/2500</math>) OR <math>0.001(2)</math> [may be unsupported].</p>

3.(a)	-5	B1	
3.(b)	At least 7 correct plots and no incorrect plot. A smooth curve drawn through their plots.	P1 C1	F.T. 'their (1,-5) Allow $\pm \frac{1}{2}$ a small square'. F.T. 'their 8 plots'. OR a curve through the 7 given points and (1,-5) Allow intention to pass through their plots. ( $\pm 1$ small square horizontal or vertical.)
3.(c)(i)	Line $y + x = 4$ drawn.	B2	B1 for a straight line going through(0,4) or (4,0) BUT NOT line $y = 4$ nor line $x = 4$
3(c)(ii)	-2.4 AND 3.4	B1	F.T. intersection of 'their curve' with 'their $y + x = 4$ ' (even for line $y = 4$ ) only if exactly two points of intersection. Must be seen to intersect their curve at two points. Allow $\pm 0.4$ small square

<p>17.</p> 	<p><math>k(k^2p - p^3)</math> OR <math>p(k^3 - kp^2)</math> is B0</p> <p>B1 If more than one graph indicated, award B0.</p>
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<p>12.(a) <math>2(2x + 3)(2x - 3)</math></p>	<p><b>B3</b> Award B3-1 for a correct answer followed by further incorrect work.</p> <p>Award B2 for the sight of any one of the following:</p> <ul style="list-style-type: none"> <li>• <math>(4x + 6)(2x - 3)</math></li> <li>• <math>(4x - 6)(2x + 3)</math></li> <li>• <math>8(x + 3/2)(x - 3/2)</math></li> <li>• <math>(2x + 3)(2x - 3)</math></li> <li>• <math>2(2x + 3)(2x + 3)</math></li> <li>• <math>2(2x - 3)(2x - 3)</math></li> </ul> <p>Award B1 for the sight of any one of the following:</p> <ul style="list-style-type: none"> <li>• <math>2(4x^2 - 9)</math></li> <li>• <math>8(x^2 - 9/4)</math></li> <li>• <math>(4x + 6)(2x + 3)</math></li> <li>• <math>(4x - 6)(2x - 3)</math></li> <li>• <math>(x + 3/2)(x - 3/2)</math></li> </ul> <p>If no marks:                  Allow SC2 for <math>(2\sqrt{2}x + 3\sqrt{2})(2\sqrt{2}x - 3\sqrt{2})</math> o.e. OR other valid, equivalent 'factorisation', e.g. <math>(8x - 12)(x + 1.5)</math> o.e.                  Allow SC1 for <math>(\sqrt{8}x + \sqrt{18})(\sqrt{8}x - \sqrt{18})</math> o.e.</p>
<p>12.(b) <math>3/2</math> AND <math>-3/2</math></p>	<p><b>B1</b> Or equivalent for either roots.                  FT if possible, provided exactly 2 possible distinct solutions.</p>
<p>12.(c) A <u>positive</u> quadratic curve passing through <math>(0, -18)</math> as a minimum with <math>-18</math> indicated on the y-axis AND passing through <math>(-3/2, 0)</math> and <math>(3/2, 0)</math> which are indicated on the x-axis.</p> 	<p><b>B2</b> FT for x-axis intersections, provided exactly 2 possible distinct solutions.</p> <p>Award B1 for any one of the following:                  A positive quadratic curve passing through <math>(0, -18)</math> as a minimum with <math>-18</math> indicated on the y-axis                  OR                  A quadratic curve (either positive or negative) passing through <math>(-3/2, 0)</math> and <math>(3/2, 0)</math> which are indicated on the x-axis.</p> <p>If the conditions for B2 are met, then only allow B1 for concave and/or convex curvature above the x-axis.</p>