

# REVISE

.wales

## 2.01 – Place value, rounding & significant figures

*Mark schemes for the 2.01 question pack*

*Spec 1.1.1, 1.1.2, 1.1.3, 1.1.4, 1.1.5 – Unit 2*

**SOLUTIONS · 2025 SPECIFICATION**

*Mark schemes for the 37 questions in the corresponding revise.wales question pack (145 marks total). Sources: legacy WJEC GCSE papers, WJEC SAM, and custom-authored mark schemes. Pack layout © revise.wales.*

2.(a)	6            -3		B2	B1 for each.
2.(b)	7 correct plots. Curve drawn.		P1 C1	<u>Use overlay.</u> F.T. 'their (-1,6)' and 'their (2,-3)'. Allow $\pm$ '½ a small square'. F.T. 'their plots'. At least 6 plots required. Clear intention to draw a curve through 'their plotted points'.
2.(c)	-0.9    and    3.4		B2	B1 for each. Allow (-0.9, 5) and (3.4, 5). F.T. intersection of 'their curve' with $y = 5$ provided exactly 2 intersections seen on graph. Allow $\pm$ '½ a small square'.  <u>If no marks gained</u> then SC1 for either of the following. $y = 5$ drawn correctly, OR <u>Two</u> correct F.T. values given for 'their straight line' and 'their curve' provided exactly 2 intersections seen on graph.
2.(d)	$2x^2 - 5x - 6 = 0$		B1	

Autumn 2016		
3(a) 605 cm	B1	
3(b) 249.5 cm	B1	
3(c) Consistent use of units for comparison, e.g. desk 200cm if another measure is given in cm	B1	<u>Penalise -1 only the use of the 'their desk' ≠ 200</u> Accept comparison with one other length, e.g. sight of 2000mm = 200cm is sufficient if any other working seen in cm (irrespective of use of bounds)
<b>Use of</b> 147.5 (cm) or 250.5 (cm) or 595(cm)	B2	'Use of' can be any of these values used within a length calculation (including the bookcase, the wardrobe and either the wall or the desk), or 595(cm) used in the interpretation within a conclusion Allow 147.49'(cm) or 250.49'(cm) respectively throughout (Otherwise award:) B1 for sight of 147.5 (cm), 250.5 (cm) or 595(cm)
Correctly evaluated calculation which could be interpreted to show the desk (200cm) would not fit, i.e. a counter example showing the desk can not fit	B1	Interpretation is not required for this B1, it is a calculation (showing that the wall or the gap is of insufficient length, i.e.) with an answer >595(cm) or <200(cm) as appropriate <u>Examples</u> (In cm, but working in m or mm is also accepted) <i>Giving an answer &gt;595:</i> $147.5 + 250.5 + 200 = 598$ , or $147 + 250 + 200 = 597$ , or $146.5 + 249.5 + 200 = 596$ OR <i>Giving an answer &lt;200:</i> $595 - 250.5 - 147.5 = 197$ , or $595 - 250 - 147 = 198$ , or $595 - 249.5 - 146.5 = 199$ i.e. working with lengths in the inclusive ranges 146.5 to 147.5 and 249.5 to 250.5 is accepted, condoning mix of upper and lower bounds provided the calculation leads to >595 or <200 appropriately
Conclusion from a correct interpretation of a correctly evaluated calculation, e.g. 'no, not certain as greater than the least length of the wall which is 595(cm)', 'no, 197(cm) is less than the length of the desk which is 200(cm)', 'no, 598(cm) > 595(cm)'	E1	This E1 depends on the award of the previous B1 Sight of 200(cm) or 595(cm) as appropriate for the comparison is required, i.e. 'no, not certain as greater than the least length of the wall' or 'no, 197 cm is less than the length of the desk' would only be awarded E1 if 595(cm) or 200(cm) respectively, has been seen previously



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Conclusion from a correct interpretation of a correctly evaluated calculation, e.g. 'no, not certain as greater than the least length of the wall which is 595(cm)', 'no, 197(cm) is less than the length of the desk which is 200(cm)', 'no, 598(cm) > 595(cm)'	E1	This E1 depends on the award of the previous B1 Sight of 200(cm) or 595(cm) as appropriate for the comparison is required, i.e. 'no, not certain as greater than the least length of the wall' or 'no, 197 cm is less than the length of the desk' would only be awarded E1 if 595(cm) or 200(cm) respectively, has been seen previously

<p>5(a)(i) Mid points : 1.5, 3, 4.5, 7</p> $1.5 \times 2 + 3 \times 6 + 4.5 \times 8 + 7 \times 4$ $= 3 + 18 + 36 + 28 = 85$ <p style="text-align: right;">+ 20</p> <p style="text-align: center;">4.25 (microns)</p>	<p>B1</p> <p>M1</p> <p>m1</p> <p>A1</p>	<p>FT 'their mid points' provided each one lies within the appropriate group, including bounds</p> <p>Accept 4.3 from correct working, i.e. <math>85 \div 20</math> seen in working Do not accept 4.2 unless <math>4.25</math> or <math>85 \div 20</math> seen in working</p>
<p>5(a)(ii) 45 dust particles means <math>3 \times 7 : 3 \times 8</math> 21 : 24 or 21 in total equivalent (A further) 13 (dust particles)</p>	<p>M1</p> <p>m1</p> <p>A1</p>	<p>Accept <math>7 \times 45 / (7+8) : 8 \times 45 / (7+8)</math></p> <p>Allow M1, m1, A0 for sight of <math>8 + 13 = 21</math></p> <p><i>Alternative:</i> <i>Trial &amp; improvement, e.g.</i> <i>18 : 27 (is 2 : 3 incorrect)</i> <i>19 : 26 (incorrect)</i> <i>20 : 25 (is 4 : 5 incorrect)</i> <i>21 : 24 (is 7 : 8 correct!!)</i></p> <p><i>M1 for sight from the above list:</i> <i>a trial with correct simplification shown</i> <b>AND</b> <i>--- either for a second trial with correct simplification shown</i> <i>--- or the second trial has clearly been dismissed</i> <i>m1 Selection of 21 : 24</i> <i>A1 (a further) 13 (dust particles)</i></p>

GCSE Mathematics – Numeracy Unit 2: Higher Tier Autumn 2016	Mark	Comment
5(b) (Circumference) $5 = 2 \times \pi \times r$ or $5 = \pi \times d$ Radius of the cylinder $\frac{5}{2\pi}$	M1 A1	$(5/2\pi = 0.79577\dots)$
Volume $\pi \times (5/2\pi)^2 \times 2$  4 (microns <sup>3</sup> )	m1 A2	FT 'their r' provided M1 awarded provided 'their r' $\neq 5/\pi$ A1 for $25/2\pi$ or 3.9(...) or 4.0 (microns <sup>3</sup> )

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1.(a)	25.1		B2	B1 for 25(.....).
4.5)	44.0		B2	B1 for 44.0 (B1 for 44.0/.....)

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<b>GCSE MATHEMATICS</b> Unit 2 : Higher tier Summer 2017	✓	Mark	<b>MARK SCHEME</b> Comments
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2.(a)	= 0.16 or equivalent. -4	A1 B1	
2.(b)	At least 6 correct plots and <u>no incorrect plot</u> . A smooth <u>curve</u> drawn through their plots.	P1 C1	F.T. 'their (3,-4)'. Allow $\pm$ '½ a small square'. F.T. 'their 7 plots'. OR a curve through the 6 given points and (3,-4). Allow intention to pass through their plots. ( $\pm$ '1 small square horizontal or vertical').
2.(c)	Line $y = -3$ drawn  1.4 AND 3.6	B1  B1	F.T. intersection of 'their curve' with 'their $y = -3$ ' only if exactly two points of intersection.

<p>5.(a) <math>(\text{Length}^2 =) 44^2 - 16^2</math> or  <math>44^2 = \text{Length}^2 + 16^2</math>  <math>(\text{Length} =) \sqrt{1680}</math> or <math>\text{Length}^2 = 1680</math>  41 (inches)</p>	M1 A1 A2	2 sig.fig. is required A1 for 41.0, 41.00 or 40.9878... rounded or truncated FT from M1 for the correctly evaluated square root of 'their 1680' provided 'their answer' < 44 (inches) for possible A2 or A1
<p>5.(b) <math>(100 \times) 710.40 \div 74</math>  (£)960</p>	M1 A1	
<p>5.(c)(i) 23.52 p</p>	B1	
<p>5.(c)(ii) 27.44 p</p>	B1	

<p>3.</p> <p>(Balls of wool per pair) <math>135 \div 20</math> (<math>\times 40</math>)          6.75 (balls) or 7 (balls) or          270 (balls) or 280 (balls)</p> <p>(Costs are <math>40 \times</math>) <math>1.42 \times 135 \div 20</math> (<math>+(40 \times) 8</math>)</p> <p>(Profit = Sales – Costs), e.g.          (Profit per pair) <math>18.95 - 1.42 \times 135 \div 20 - 8</math>          OR          (Profit for 40 pairs)  <math>40 \times 18.95 - 40 \times (1.42 \times 135 \div 20 + 8)</math>          OR          Appropriate amounts used to calculate  <math>(100 \times) \frac{\text{total sales}}{\text{total costs}} - 1(\times 100)</math></p> <p>Use of appropriate amounts to calculate:          (Percentage profit = <math>100 \times</math>) <math>\frac{\text{profit}}{\text{costs}}</math>          or <math>(100 \times) \frac{\text{sales}}{\text{costs}} - 1(\times 100)</math></p> <p style="text-align: center;">7.8(%) or 5.6(%)</p> <p>See next page for OCW strands.</p>	<p>M1 A1</p> <p>m1</p> <p>M2</p> <p>m1</p> <p>A1</p>	<p>Accept rounding or truncation of 1/2p throughout</p> <p>FT <math>135 \div 20 = 6.75</math> balls and 7 balls</p> <table border="1" style="width: 100%;"> <tr> <td>Costs</td> <td>1 pair</td> <td>40 pairs</td> </tr> <tr> <td>6.75 balls</td> <td>£9.585</td> <td>£383.40</td> </tr> <tr> <td>7 balls</td> <td>£9.94</td> <td>£397.60</td> </tr> </table> <p><b>Profit using 6.75 balls</b></p> <table border="1" style="width: 100%;"> <tr> <td>1 pair</td> <td><math>18.95 - 9.585 - 8</math> <math>= 18.95 - 17.585 = \text{£}1.365</math></td> </tr> <tr> <td>40 pairs</td> <td><math>758 - 383.40 - 320</math> <math>= 758 - 703.40 = \text{£}54.60</math></td> </tr> </table> <p><b>Profit £, using 7 balls</b></p> <table border="1" style="width: 100%;"> <tr> <td>1 pair</td> <td><math>18.95 - 9.94 - 8</math> <math>= 18.95 - 17.94 = \text{£}1.01</math></td> </tr> <tr> <td>40 pairs</td> <td><math>758 - 397.60 - 320</math> <math>= 758 - 717.60 = \text{£}40.40</math></td> </tr> </table> <table border="1" style="width: 100%;"> <tr> <td>M1 for any 1 amount</td> <td>Amount, £</td> </tr> <tr> <td>Paying sister 40 prs</td> <td>320</td> </tr> <tr> <td>Total sales 40prs</td> <td>758</td> </tr> <tr> <td colspan="2">Total costs 40prs:</td> </tr> <tr> <td style="text-align: right;">6.75 balls</td> <td>703.4(0)</td> </tr> <tr> <td style="text-align: right;">7 balls</td> <td>717.6(0)</td> </tr> <tr> <td colspan="2">Total cost 1 pair:</td> </tr> <tr> <td style="text-align: right;">6.75 balls</td> <td>17.585</td> </tr> <tr> <td style="text-align: right;">7 balls</td> <td>17.94</td> </tr> </table> <p>OR</p> <p>M1 for any 1 of the following:</p> <ul style="list-style-type: none"> <li>omitting to pay her sister:  <math>18.95 - 1.42 \times 135 \div 20</math> or  <math>40 \times 18.95 - 40 \times (1.42 \times 135 \div 20)</math></li> <li>inconsistent use of <math>\times 40</math>:  <math>40 \times 18.95 - 1.42 \times 135 \div 20 - 8</math> or  <math>18.95 - 40 \times (1.42 \times 135 \div 20 + 8)</math></li> </ul> <p>m1 FT from previous M1 or M2          FT <math>18.95 - \text{'their cost per pair'}</math> OR          'their cost per pair'</p> <p><u><math>40 \times \text{'their 18.95'}</math> – 'their total costs'</u>          'their total costs'</p> <p>OR equivalent</p> <p>A1 No other FT, must be 2 s.f.          7.8% CAO comes from use of 6.75 balls,          5.6% CAO comes from use of 7 balls</p>	Costs	1 pair	40 pairs	6.75 balls	£9.585	£383.40	7 balls	£9.94	£397.60	1 pair	$18.95 - 9.585 - 8$ $= 18.95 - 17.585 = \text{£}1.365$	40 pairs	$758 - 383.40 - 320$ $= 758 - 703.40 = \text{£}54.60$	1 pair	$18.95 - 9.94 - 8$ $= 18.95 - 17.94 = \text{£}1.01$	40 pairs	$758 - 397.60 - 320$ $= 758 - 717.60 = \text{£}40.40$	M1 for any 1 amount	Amount, £	Paying sister 40 prs	320	Total sales 40prs	758	Total costs 40prs:		6.75 balls	703.4(0)	7 balls	717.6(0)	Total cost 1 pair:		6.75 balls	17.585	7 balls	17.94
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Unit 2 : Higher Tier Summer 2018		.....	-----
1.(a)	8.27	B2	Mark final answer. B1 for sight of 8.26(.....) or for sight of 8.270 or for sight of 8.30 or for sight of 8.3
1.(b)	0.0213	B2	Mark final answer. B1 for sight of 0.0212(.....) Leave as fraction if

<p>2.(c) 280°</p> <p>3.</p> <p>One correct evaluation <math>4 \leq x \leq 5</math>                  2 correct evaluations <math>4.25 \leq x \leq 4.45</math>,                  one <math>&lt; 0</math>, one <math>&gt; 0</math>.                  2 correct evaluations <math>4.25 \leq x \leq 4.35</math>,                  one <math>&lt; 0</math>, one <math>&gt; 0</math>.</p> <p>(x = ) 4.3</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>Correct evaluation regarded as enough to identify if negative or positive. If evaluations not seen accept 'too high' or 'too low'.</p> <p>Look out for equating <math>x^3 - 7x = 51</math></p> <table border="0"> <tr> <td><math>x</math></td> <td><math>x^3 - 7x - 51</math></td> <td></td> <td></td> </tr> <tr> <td>4</td> <td>-15</td> <td></td> <td></td> </tr> <tr> <td>4.1</td> <td>-10.779</td> <td></td> <td></td> </tr> <tr> <td>4.2</td> <td>-6.312</td> <td>4.25</td> <td>-3.984...</td> </tr> <tr> <td>4.3</td> <td>-1.593</td> <td>4.34</td> <td>0.366...</td> </tr> <tr> <td>4.4</td> <td>3.384</td> <td>4.35</td> <td>0.862...</td> </tr> <tr> <td>4.5</td> <td>8.625</td> <td>4.45</td> <td>5.971...</td> </tr> <tr> <td>4.6</td> <td>14.136</td> <td></td> <td></td> </tr> <tr> <td>4.7</td> <td>19.923</td> <td></td> <td></td> </tr> <tr> <td>4.8</td> <td>25.992</td> <td></td> <td></td> </tr> <tr> <td>4.9</td> <td>32.349</td> <td></td> <td></td> </tr> <tr> <td>5</td> <td>39</td> <td></td> <td></td> </tr> </table> <p>For this question A1 can only be awarded if M1 given.</p>	$x$	$x^3 - 7x - 51$			4	-15			4.1	-10.779			4.2	-6.312	4.25	-3.984...	4.3	-1.593	4.34	0.366...	4.4	3.384	4.35	0.862...	4.5	8.625	4.45	5.971...	4.6	14.136			4.7	19.923			4.8	25.992			4.9	32.349			5	39		
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<p>Organisation and Communication</p> <p>Accuracy of writing</p>	<p>OC1</p> <p>W1</p>	<p>For OC1, candidates will be expected to:</p> <ul style="list-style-type: none"> <li>• present their response in a structured way</li> <li>• explain to the reader what they are doing at each step of their response</li> <li>• lay out their explanation and working in a way that is clear and logical</li> </ul> <p>For W1, candidates will be expected to:</p> <ul style="list-style-type: none"> <li>• show all their working</li> <li>• make few, if any, errors in spelling, punctuation and grammar</li> <li>• use correct mathematical form in their working</li> </ul>																																																

<p>8. <math>2x - y = 6</math> or equivalent  e.g. <math>12(2x - y) = 72</math>  <math>3x + y = 16.5</math> or equivalent  e.g. <math>3x + y + 3x + y = 33</math></p> <p>Correct method to solve simultaneous equations.</p> <p style="text-align: center;"><math>x = 4.5</math>  <math>y = 3</math></p>	<p>B1  B1  M1  A1  A1</p>	<p>B1 for sight of correct equation.</p> <p>B1 for sight of correct equation.  FT 'their two simultaneous equations'.</p> <p>M1 Equating a variable (if necessary) AND adding or subtracting as appropriate. Allow one slip.</p> <p>A1 C.A.O. from 'their equations' for 1<sup>st</sup> variable.</p> <p>A1 F.T. from substituting 'their 1<sup>st</sup> variable' if M1 gained.</p> <p>SC1 if <math>x = 4.5</math> AND <math>y = 3</math> given without using simultaneous equations method. This could happen after a B1 (or B1B1) gained or just appear with no equations shown.</p>
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<p>10(a) <math>\frac{6 \times 10^9}{1.5 \times 10^8}</math> or equivalent</p> <p>40 or <math>4 \times 10^1</math></p>	<p>M1</p> <p>A1</p>	<p>A calculation, using approximations, that would lead to an answer of <math>&lt; 50</math></p> <p>FT their calculation e.g. <math>\frac{5.9 \times 10^9}{1.5 \times 10^8}</math> leads to an answer of 39.33</p>
<p>10(b)</p> <p><math>63000 \times 1.5 \times 10^8</math> OR <math>60000 \times 1.496 \times 10^8</math> OR <math>60000 \times 1.5 \times 10^8</math></p> <p><math>= 9.4(5) \times 10^{12}</math> (km) OR <math>8.9(76) \times 10^{12}</math> (km) OR <math>9 \times 10^{12}</math> (km)</p>	<p>M2</p> <p>A1</p>	<p>Acceptable options for M2 and A1 Award M1 only for <math>63000 \times 1.496 \times 10^8</math> Or M1 for 1 slip in the power of 10, but otherwise correct</p> <p>FT from M2 only If no marks awarded, SC1 for <math>6(.3) \times 10^{12}</math> (km)</p>

11. $13200 \times 460 \div 3$ $= 2.024(m^3)$ $\quad\quad\quad = 2024000 (cm^3)$	M1 A1 B1	solving an equation. Or equivalent. Strict FT of a correct conversion of their volume to $m^3$ .
<u>Alternative method</u> Sight of 1.32 AND 4.6 $1.32 \times 4.6 \div 3$ $= 2.024(m^3)$	B1 M1 A1	FT 'their 1.32' and 'their 4.6' from place value errors for M1A1.

13.	$\frac{26.5-1.95}{0.815} \text{ or } \frac{24.55}{0.815}$	M2	<p>If many attempts are offered without a method/answer being identified then mark final attempt.</p> <p>Award M1 for correct use of values <math>26.5 \leq a &lt; 27</math>, <math>1.9 &lt; b \leq 1.95</math> and <math>0.81 &lt; c \leq 0.815</math>.</p> <p>OR award M1 for use of 2 of the 3 correct limits.</p>
	$= 30(.12\dots)$	A1	<p>Mark final answer. Only award A1 if M2 gained.</p> <p>If no marks gained award SC1 for an unsupported answer of 30.12(...).</p> <p>Unsupported 30 or 30.1 gives no marks</p>

14. Attempt to find a [face diagonal] <sup>2</sup> . $\sqrt{3^2 + 5^2 + 7^2} (= \sqrt{83})$ $= 9.11(\text{cm})$	S1 M2 A1	E.g. $3^2 + 5^2 = 34$ OR $3^2 + 7^2 = 58$ OR $5^2 + 7^2 = 74$ M1 for $3^2 + 5^2 + 7^2$ . May be seen in stages. This mark implies S1. CAO (must be correct to 2 decimal places). Unsupported answer of $\sqrt{83}$ gains S1 M2 A0.
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Unit 2: Higher Tier	.....	-----
<p>1. Sight of 9.95 (m) or 99.95(m) or 995 (cm) or 9995 (cm)</p> <p>(Least length) 9.95 + 99.95 + 9.95 or equivalent in cm</p> <p style="text-align: center;">119.85 (m)</p>	<p>B1</p> <p>M1</p> <p>A1</p>	<p>If units are given they must be correct</p> <p>FT 'their least measurements' x and y, provided <math>9.9 (m) \leq x &lt; 10(m)</math> and <math>99.9 (m) \leq y &lt; 100(m)</math> as appropriate</p> <p>CAO Award all 3 marks for a correct response</p> <p>If no marks, award SC1 for an answer of 118.5(m) or 119.985(m) or <math>(9.95 + 9.95 + 99.5 =) 119.4(m)</math></p>
<p>1. <i>Alternative method:</i> <math>100 + 10 + 10 - 3 \times 0.05</math> or equivalent in cm 119.85 (m)</p>	<p>M2</p> <p>A1</p>	<p>M1 for sight of - 5 cm or -0.05 (m) used</p> <p>CAO If no marks, award SC1 for an answer of 119.7.(m)</p>



4.(a)	an expression	B1	
4.(b)	an equation	B1	
5.	(Mid-points) 2·5, (7·5), 12·5 and 17·5. $8 \times 2\cdot5 + (0 \times 7\cdot5) + 7 \times 12\cdot5 + 5 \times 17\cdot5$ $( 20 + 0 + 87\cdot5 + 87\cdot5 = 195)$ $\div 20$ $= 9\cdot75$	B1 M1  m1 A1	Allow for sight of mid-points. F.T. 'their mid-points' including bounds, provided they fall within the classes (including lower and upper bounds and used consistently). C.A.O.
6.	( x = ) $\frac{360}{15}$ or $180 - \frac{(15-2) \times 180}{15}$ or equivalent $= 24(^{\circ})$ (BR = ) $8 \times \cos 24$ or $8 \times \sin (90 - 24)$ $= 7\cdot3(0\dots)(\text{cm})$ or $7\cdot31(\text{cm})$	M1  A1 M2  A1	May be seen in parts.  FT 'their stated value for x' ( x < 90°) M1 for $\frac{BR}{8} = \cos 24$ or $\frac{BR}{8} = \sin (90 - 24)$ Accept equivalent of using sin rule (as sin 90 = 1).  <u>Alternative method to find BR</u> A correct and complete method (using two trigonometric relationships and possibly Pythagoras's theorem) M2 $BR = 7\cdot3(0\dots)(\text{cm})$ or $7\cdot31(\text{cm})$ A1
7.	$2\cdot656 \times 10^6$	B2	B1 for a correct value but not in standard form. Mark final answer. B1 for sight of 2 656 000. SC1 for $2\cdot66 \times 10^6$ or $2\cdot7 \times 10^6$ or $2\cdot6 \times 10^6$ or $2\cdot65 \times 10^6$
8.	Sight of 24·5 AND 15·5 OR Sight of 23·5 AND 14·5  $2(24\cdot5 + 15\cdot5) - 2(23\cdot5 + 14\cdot5)$ or equivalent  $= 4(\text{cm})$	B1  M1  A1	Sight of (Greatest =) 80 <u>OR</u> (Least =) 76 implies B1  FT only for upper bounds of 24·4 AND 15·4 or 24·49 AND 15·49 (lower bounds must be 23·5 AND 14·5 else M0)  CAO If M0, award B1 and an SC1 for sight of (Greatest =) 80 <u>AND</u> (Least =) 76
	<u>Alternative method.</u> Difference between least and greatest length for each side = 1(cm) $4 \times 1$  $= 4(\text{cm})$	B1  M1  A1	  FT only for differences of 0·9 or 0·99  CAO
9.	Method to eliminate variable e.g. equal coefficients with <u>appropriate</u> addition or subtraction. First variable found, x = 4 or y = -1. Substitute to find the 2 <sup>nd</sup> variable. Second variable found	M1  A1 m1 A1	No marks for trial and improvement. Allow 1 error in one term, not the term with equal coefficients.  C.A.O. F.T. their '1 <sup>st</sup> variable'.  Award no marks for unsupported correct answers.

<p>11.</p> $\frac{63 \cdot 5^2}{8 \cdot 65}$ <p>= 466(·156...) or 466·16 or 466·2</p>	<p>M2</p> <p>A1</p>	<p>If many attempts are offered without a method/answer being identified, then mark the final attempt.</p> <p>If M2 not gained, award M1 for correct use of values <math>63 \leq d &lt; 64</math> AND <math>8 \cdot 6 &lt; e \leq 8 \cdot 7</math></p> <p>Mark final answer. M2 required for A1.</p> <p>Fractional equivalent <math>466(\cdot 156 \dots) = 80645/173</math></p> <p>Allow this A1 for an answer of 470 only from correct unambiguous working seen.</p> <p>If no marks gained, award SC1 for sight of 63·5 and 8·65 used within the same calculation.</p>
<p>12. Use of cosine rule followed by sine rule</p> <p>(EG = ) <math>\sqrt{2 \cdot 7^2 + 3 \cdot 2^2 - 2 \times 2 \cdot 7 \times 3 \cdot 2 \times \cos 79^\circ}</math></p> <p>(EG =) 3·77.... (cm)</p> <p><math>\sin EFG = EG \times \sin 65^\circ / 6 \cdot 4</math> OR <math>EFG = \sin^{-1}(EG \times \sin 65^\circ / 6 \cdot 4)</math></p> <p>F = 32(·29.....°)</p>	<p>S1</p> <p>M2</p> <p>A1</p> <p>M2</p> <p>A1</p>	<p>M1 for <math>(EG^2 =) 2 \cdot 7^2 + 3 \cdot 2^2 - 2 \times 2 \cdot 7 \times 3 \cdot 2 \times \cos 79^\circ</math> or for <math>(EG^2 =) 14 \cdot 2(3 \dots)</math></p> <p>Accept 3·8 cm</p> <p>Allow <math>\sqrt{14 \cdot 2(3 \dots)}</math> if used in this form in subsequent work, provided not evaluated as a decimal (at any stage)</p> <p>F.T. 'their derived EG' (not 2·7, 3·2, 6·4 or spurious EG).</p> <p>Award M1 for <math>\sin EFG / EG = \sin 65^\circ / 6 \cdot 4</math> OR <math>EG / \sin EFG = 6 \cdot 4 / \sin 65^\circ</math></p> <p>Dependent on previous M2.</p>
<p>13. (Numerator) Sight of <math>3x(2x - 3)</math> (Denominator) Sight of <math>(2x - 3)(2x + 3)</math></p> $\frac{3x}{2x + 3}$	<p>B1</p> <p>B2</p> <p>B1</p>	<p>B1 for <math>(2x \dots 3)(2x \dots 3)</math></p> <p>Mark final answer.</p> <p>F.T. provided at least one previous B1 awarded AND provided simplification required.</p>
<p>14. (a) <math>\frac{1}{2} \times (x - 1) \times (2x + 3) \times \sin 30^\circ [= 6]</math> OR <math>\frac{1}{2} \times (2x^2 + 3x - 2x - 3) \times \sin 30^\circ [= 6]</math></p> <p><math>2x^2 + x - 3 (= 6 \times 2 \times 2)</math></p> <p><math>2x^2 + x - 27 = 0</math></p>	<p>B1</p> <p>B1</p> <p>B1</p>	<p>Use of 'Area = <math>\frac{1}{2} ab \sin C</math>'.</p> <p>Correct expansion of brackets and correct collection of x terms. May be implied within equation.</p> <p>Must be convincing.</p>
<p>14. (b) <math>(x =) \frac{-1 \pm \sqrt{(1)^2 - 4(2)(-27)}}{2(2)}</math></p> <p><math>(x =) \frac{-1 \pm \sqrt{217}}{4}</math></p> <p>(x =) -3·93 AND 3·43</p>	<p>M1</p> <p>A1</p> <p>A1</p>	<p><b>This substitution into the formula must be seen for M1, otherwise award M0A0A0.</b></p> <p>Allow one slip in substitution <b>for M1 only</b>, but must be correct formula.</p> <p>Can be implied from at least one correct value of x evaluated, provided M1 awarded.</p> <p>Both solutions required.</p> <p><u>Using trial and improvement</u> Award B3 for a method leading to <u>both</u> solutions, namely <math>x = -3 \cdot 93</math> AND <math>x = 3 \cdot 43</math>, otherwise B0.</p> <p>An unsupported answer gains zero marks.</p>
<p>14. (c) (AC = ) 2·43 (cm)</p> <p>Length cannot be negative / must be positive.</p>	<p>B1</p> <p>E1</p>	<p>F.T. 'their derived x' provided one positive and one negative solution.</p> <p>Accept any valid explanation, e.g. <math>x - 1 &gt; 0</math>, so <math>x &gt; 1</math>, <math>x</math> cannot be negative (as <math>x - 1</math> must be <math>&gt; 0</math>)</p>
<p>15. (a) <math>y = f(x) - 3</math></p>	<p>B1</p>	
<p>15. (b) <math>y = -f(x)</math></p>	<p>B1</p>	
<p>15. (c) <math>y = f(x - 10)</math></p>	<p>B1</p>	

<p>10.</p> $\frac{97.5}{0.55}$ $= 177.3$	<p>M2</p> <p>A1</p>	<p>If many attempts are offered without a method/answer being identified, then mark the final attempt.</p> <p>If M2 not gained, award M1 A0 for correct use of values <math>97.5 \leq t &lt; 98</math> and <math>0.5 &lt; w \leq 0.55</math>.</p> <p>CAO. Must be to 1 decimal place. Mark final answer. An unsupported answer of 177.3 gains full marks. SC2 for an unsupported answer of 177.27(2727...), fractional equivalent = 1950/11 SC1 for an unsupported answer of 177 or 177.2 or for sight of 97.5 and 0.55 used within the same calculation.</p>
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<p>16. (Sight of <math>2x(5x + 1) = 10x^2 + 2x</math> OR (Sight of <math>(7 - 2x)^2 = 49 - 14x - 14x + 4x^2</math> OR <math>2x(5x + 1) = (7 - 2x)^2</math>)</p> $10x^2 + 2x = 49 - 14x - 14x + 4x^2$ $6x^2 + 30x - 49 = 0$ $x = \frac{-30 \pm \sqrt{30^2 - 4 \times 6 \times -49}}{2 \times 6} \quad \text{OR} \quad x = \frac{-30 + \sqrt{30^2 - 4 \times 6 \times -49}}{2 \times 6}$ $x = \frac{-30 \pm \sqrt{2076}}{12} \quad \text{OR} \quad x = \frac{-30 + \sqrt{2076}}{12}$ $\text{OR} \quad x = \frac{-15 \pm \sqrt{519}}{6} \quad \text{OR} \quad x = \frac{-15 + \sqrt{519}}{6}$ <p><math>x = 1.3</math> (answer to 1 d.p.)</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>Or equivalent. Or equivalent. <math>2x(5x + 1) = (7 - 2x)^2</math> may be implied in later working.</p> <p>F.T. expansions of equivalent level of difficulty provided B1 previously awarded. '= 0' required, but may be implied by an attempt to use the quadratic formula.</p> <p>Substitution into the formula must be seen for M1. F.T. 'their derived quadratic equation' equated to zero of equivalent difficulty (<math>a</math>, <math>b</math> and <math>c</math> must be non-zero). Allow one slip in substitution <b>for M1 only</b>, but must be correct formula.</p> <p>Can be implied from at least one of their two values of <math>x</math> correctly evaluated (<math>x=1.29\dots</math> or <math>x=-6.29\dots</math>)</p> <p>FT for A1 for their quadratic equation provided:</p> <ul style="list-style-type: none"> <li>• rounding required to 1 d.p. AND</li> <li>• one positive and one negative root.</li> </ul> <p>Do not allow 1.30. Do not penalise if negative solution also shown (<math>x = -6.3</math> or <math>-6.29(\dots)</math>)</p> <p>Note: sight of a correct answer does not imply full marks without working.</p>
<p><u>Using trial and improvement for the final 3 marks</u> Two correct evaluations <math>1.25 \leq x \leq 1.35</math>, (one value <math>&lt; 0</math>, one value <math>&gt; 0</math>)</p> <p><math>x = 1.3</math> (answer to 1 d.p.)</p>	<p>M2</p> <p>A1</p>	<p>Two correct evaluations must be seen, otherwise M0. F.T. 'their derived quadratic equation' (<math>=0</math> or '<math>=</math>their constant') of equivalent difficulty (<math>a</math>, <math>b</math> and <math>c</math> must be non-zero) and their <math>x</math> involves rounding to 1 d.p.</p> <p>FT for A1 for their quadratic equation.</p>

<p>3(a) <math>4500 \times (1 - 0.2(0)) \times (1 - 0.14)^9</math> or <math>4500 \times 0.8(0) \times 0.86^9</math> or equivalent</p> <p>An answer in the range (£)926.35 to (£)926.40</p>	<p>M2</p> <p>A1</p>	<p>For M2, do not ignore any additional years considered, unless 10 years selected or implied in later working</p> <p>M1 for equivalent of one of the following (which may be embedded in other working):</p> <ul style="list-style-type: none"> <li>• <math>4500 \times (1 - 0.2(0))</math> (= 3600)</li> <li>• <math>4500 \times 0.8(0)</math> (= 3600)</li> <li>• <math>4500 \times (1 - 0.14)^9</math> (= 1157.97...)</li> <li>• <math>4500 \times 0.86^9</math> (= 1157.97...)</li> </ul> <p>An answer for 10 years (not beyond) must be selected</p> <p>Allow an answer of (£)926 provided not from rounding an amount outside the range given</p> <p>Award M1, SC1 for an answer (<math>4500 \times 0.8 \times 0.86^{10} =</math>) (£)796.68(5.... ) or (£)796.69 or (£)796.70 or (£)797</p>
<p>3(b) <math>100 \times 750 \div 125</math> or <math>100 \times \frac{750}{125}</math> or equivalent (£) 600</p>	<p>M1</p> <p>A1</p>	<p>Answer space takes precedence</p>
<p>3(c)</p> <p>Sight of appropriate 80 (cm) (height of triangle)</p> <p>(<math>\frac{1}{2}</math> width =) <math>\frac{80}{\tan 33^\circ}</math> or (<math>\frac{1}{2}</math> width =) <math>80 \times \tan (90^\circ - 33^\circ)</math></p> <p style="text-align: center;">× 2</p> <p>(Width of garage is) 246(cm) to 246.4(cm)</p>	<p>B1</p> <p>M2</p> <p>m1</p> <p>A1</p>	<p>Accept equivalents using the sine rule throughout '<math>\frac{1}{2}</math> width' may be referred to by any unknown</p> <p>Check if indicated on the diagram</p> <p>(= 123.189... cm or 123.2 cm) FT 'their 80' provided <math>\leq 120</math> and <math>\neq 90</math></p> <p>M1 for sight of <math>\tan 33^\circ = \frac{80}{\frac{1}{2} \text{ width}}</math> or <math>\tan (90^\circ - 33^\circ) = \frac{\frac{1}{2} \text{ width}}{80}</math></p> <p>FT provided at least M1 previously awarded, i.e. for intention to double 'their <math>\frac{1}{2}</math> width'</p> <p>CAO. ISW</p>
<p>3(d)</p> <p>(Maximum space =) <math>555 - 395 - 70</math> or <math>550 - 400 + 2 \times 5 - 70</math> or equivalent</p> <p style="text-align: center;">90 (cm)</p>	<p>M2</p> <p>A1</p>	<p>Check the diagram</p> <p>M1 for any of the following</p> <ul style="list-style-type: none"> <li>• use of <math>550 &lt; \text{'their 555'} \leq 560</math> AND <math>390 \leq \text{'their 395'} &lt; 400</math></li> <li>• for sight of 555 and 395</li> <li>• for sight of <math>550 - 400 + 2 \times 5</math></li> </ul> <p>CAO</p> <p>Award M1 and SC1 for an answer of <math>(555 - 395 =)</math> 160 (cm)</p>

4.(a)	1·2	B2	Mark final answer. Award B1 for one of the following: <ul style="list-style-type: none"><li>• sight of <math>1\cdot1(5519\dots)</math>.</li><li>• an answer of <math>1\cdot20</math>.</li></ul> Do not award B2 or B1 for answers obtained from incorrect work (e.g. rounding and/or estimating).
4.(b)	0·043	B2	Mark final answer. Award B1 for sight of one of the following: <ul style="list-style-type: none"><li>• <math>\frac{1}{23}</math></li><li>• <math>1 \div 23</math></li><li>• <math>0\cdot0434(\dots)</math></li><li>• <math>0\cdot0435</math></li><li>• <math>0\cdot04</math>.</li></ul>
4.(c)(i)	12	B1	
4.(c)(ii)	5	B1	

<p>6. Sight of 4(hr) 35(min) AND 2(hr) 45(min)  OR Sight of 275(min) AND 165(min)</p>		<p>B1 Allow incorrect notation for time (e.g. 4:35 for 4(hr) 35(min)).</p>
<p>OR sight of <math>2 \times 5(\text{min})</math> in an appropriate calculation.</p>		
<p>Valid method e.g.</p>		
<ul style="list-style-type: none"> <li>• 4(hr) 35(min) + 2(hr) 45(min) (=6(hr) 80(min) )</li> <li>• 275(min) + 165(min) (= 440 (min) )</li> <li>• 6 (hr) 90 (min) – 10 (min)</li> <li>• 7 (hr) 30 (min) – 10 (min)</li> <li>• 4(hr) 40(min) + 2(hr) 50(min) – 10 (min)</li> <li>• 280 (min) + 170 (min) – 10(min)</li> </ul>	<p>M1</p>	<p>If B0, FT provided unambiguously chosen:  '4h 30m <math>\leq t_1 &lt; 4h 40m</math>' and '2h 40m <math>\leq t_2 &lt; 2h 50m</math>'  OR  '270m <math>\leq t_1 &lt; 280m</math>' and '160m <math>\leq t_2 &lt; 170m</math>'  Allow incorrect notation for time (e.g. 4:35 for 4(hr) 35(min)).</p>
<p style="text-align: right;">7 (hr) 20 (min)</p>	<p>A1</p>	<p>CAO. If units are given they must be correct.  Award B1M1A0 for a final answer of 6hrs 80min, 6:80 or 7:20.</p>

<p>3(a)                  (Difference 60 million – 41 000 000 =) 19 000 000                  or 19 million</p> <p>(Underspend) <math>\frac{19\,000\,000}{60\,000\,000} (\times 100)</math> or equivalent</p> <p style="text-align: right;">31.67(%)</p>	<p>B1</p> <p>M1</p> <p>A1</p>	<p>May be implied in further working                  Allow 19 m(ii)</p> <p>FT 'their 60 million – 41 000 000' including if a place value error made</p> <p>CAO (must be 2 d.p.)                  Answer space takes precedence</p>
<p>3(a) <u>Alternative method</u>                  (Underspend)</p> <p>(100 -) <math>\frac{41\,000\,000}{60\,000\,000} (\times 100)</math> or equivalent</p> <p style="text-align: right;">31.67(%)</p>	<p>M1</p> <p>A2</p>	<p>Allow place value error</p> <p>CAO (must be 2 d.p.)                  Answer space takes precedence</p> <p>A1 for 31.6(6...%), 31.7(%), 32(%) or 68.33(%)</p>
<p>3(b) <math>4 \times 10^6</math></p>	<p>B1</p>	

<p>3(c) (Change to \$) <math>350 \times 1.25</math> <span style="float: right;">(\$)<math>437.5(0)</math></span></p> <p>(Only \$10 and \$50 notes available so he can buy) <span style="float: right;">(\$)<math>430</math></span></p> <p>(Fewest number of notes making up \$430) <span style="float: right;">8 \$50 (notes) and 3 \$10 (notes)</span></p> <p>(Cost in £ to buy \$430 is) <math>430 \div 1.25</math> or <math>350 - 7.5(0) \div 1.25 (= 350 - 6)</math> <span style="float: right;">(£)<math>344</math></span></p>	<p>M1 A1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p><i>Do not penalise slips in giving incorrect use of £ for \$</i></p> <p>FT 'their (\$)<math>437.5(0)</math>' (provided not a multiple of 10) rounded down to nearest multiple of 10 Accept stated or implied as (\$)<math>7.50</math> can't be converted (<math>\\$430</math>) implies previous M1 A1, provided not from incorrect working</p> <p>FT 'their \$430' provided it is a multiple of 10 (and provided M1 previously awarded) Must be fewest number of notes, that may be listed Sight of correct number of notes with no incorrect working implies previous A1, unless contradicted</p> <p>FT 'their whole number multiple of \$10' <math>\div 1.25</math> Ignore attempt at any further calculation if <math>430 \div 1.25</math> seen</p> <p>Must be <math>&lt;(\pounds)350</math> and depends on M1 M1 previously awarded Mark final answer</p> <p>If final M0 A0, then award SC1 for (£) 6 (left) or similar on FT, provided not from incorrect or inappropriate working</p>
<p>3(c) <u>Alternative method</u> <math>\pounds40 = \\$50</math> and <math>\pounds8 = \\$10</math> <span style="float: right;">8 \$50 notes, 3 \$10 notes</span></p> <p>(Cost to buy £350 is) <math>8 \times 40 + 3 \times 8</math> <span style="float: right;">(£)<math>344</math></span></p>	<p>M1 A3</p> <p>M1 A1</p>	<p>A2 for 8 \$50 notes <i>and sight of <math>350 - 8 \times 40</math> or equivalent</i> OR A1 for 8 \$50 notes</p>
<p>Organisation and communication</p> <p>Writing</p>	<p>OC1</p> <p>W1</p>	<p>For OC1, candidates will be expected to:</p> <ul style="list-style-type: none"> <li>• present their response in a structured way</li> <li>• explain to the reader what they are doing at each step of their response</li> <li>• lay out their explanations and working in a way that is clear and logical</li> <li>• write a conclusion that draws together their results and explains what their answer means</li> </ul> <p>For W1, candidates will be expected to:</p> <ul style="list-style-type: none"> <li>• show all their working</li> <li>• make few, if any, errors in spelling, punctuation and grammar</li> <li>• use correct mathematical form in their working</li> <li>• use appropriate terminology, units, etc.</li> </ul>

<p>6. (Width of poster) <math>2 \times \frac{26.4}{2.4}</math> or <math>2 \times 11</math> or equivalent 22 (cm)</p> <p>(Perimeter of poster <math>2 \times (22 + 26.4) =</math>) 96.8 (cm) 100 (cm)</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p>	<p>Mark final answer for the width of the poster</p> <p>FT 'their 22' provided M1 previously awarded</p> <p>FT provided 95 &lt; 'their 96.8' &lt;100, as 100 correct to 1 significant figure</p> <p>Accept working in mm or m, units must then be given in the final answer</p> <p>Do not accept an unsupported answer of 100 (cm)</p>
<p><u>6. Alternative method</u> (Perimeter of stamp) 8.8 (cm) <b>AND</b> sight of <math>\frac{26.4}{2.4} (= 11)</math> or <math>\frac{2.4}{26.4} (= \frac{1}{11})</math></p> <p>(Perimeter of poster) <math>(2 + 2.4 + 2 + 2.4) \times \frac{26.4}{2.4}</math> or <math>8.8 \times \frac{26.4}{2.4}</math> or <math>8.8 \times 11</math> or equivalent 96.8 (cm) 100 (cm)</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p>	<p>FT 'their 2 + 2.4 + 2 + 2.4'</p> <p>FT provided 95 &lt; 'their 96.8' &lt;100, as 100 correct to 1 significant figure</p> <p>Accept working in mm or m, units must then be given in the final answer</p> <p>Do not accept an unsupported answer of 100 (cm)</p>

8(a) $\frac{360 - 15 \times \pi \times 60}{360} (+60)$  $= 241 \text{ (mm)}$	M1  A2	A1 for any one of the following: <ul style="list-style-type: none"><li>• answer of 240.5(5) to 240.7</li><li>• answer of <math>\frac{115\pi}{2} + 60</math> or <math>57.5\pi + 60</math></li><li>• sight of (180.5(5) to 180.7) + 'their 60' correctly rounded to the nearest mm</li><li>• sight of 181</li></ul>
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<p>8(b)</p> <p>(Greatest possible area of a part = )</p> $\pi \times 80.5 \times 30.25 + \frac{4 \times \pi \times 30.25^2}{2}$ <p>(7646.2 to 7651.2)    (5746.59 to 5750.3)</p> <p>= 13392.79 to 13401.5    or    <math>4265.25\pi</math> (mm<sup>2</sup>)</p> <p>(Minimum number of tins needed =)</p> $20000 \times 13399.678.. \div 3950000$ <p>= 68 (tins)</p>	<p>An answer of 68 tins does not imply full marks should be awarded, as it can be a result of inaccuracy in workings</p> <p>M3</p> <p>M2 for</p> <ul style="list-style-type: none"> <li><math>\pi \times 80.5 \times 30.25 + \frac{4 \times \pi \times 30.25^2}{2}</math></li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li><math>\pi \times \text{'their 80.5'} \times \text{'their 30.25'} + \frac{4 \times \pi \times \text{'their 30.25'}^2}{2}</math></li> </ul> <p>where <math>80 &lt; \text{'their 80.5'} \leq 81</math> and <math>30 &lt; \text{'their 30.25'} \leq 30.5</math> and where 'their 30.25' could have different values in the two terms, but both have to be in the range shown</p> <p>M1 for</p> <ul style="list-style-type: none"> <li>the sum of 2 terms with 1 correct and with bounds in the same ranges as for M2</li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li><math>\pi \times 80 \times 30 + \frac{4 \times \pi \times 30^2}{2}</math> (= 4200π)</li> </ul> <p>A1</p> <p>CAO. May be implied by sight of 267 857 600 to 268 028 400 (total surface area of 20 000 parts)</p> <p>M1</p> <p>FT 'their 13399.678...' provided it has come from the use of 'their upper bounds' of 80mm and 60mm if bounds used          Allow M1 only for <math>20000 \times 13399.678.. \div \text{'their 3 950 000'}</math>          where <math>3900000 \leq \text{'their 3 950 000'} &lt; 4000000</math></p> <p>A1</p> <p>A0 for 67.8...tins</p> <p>If no marks awarded, and from a misinterpretation of the question,          SC3 for an answer of 65 tins from <math>20000 \times (\pi \times 79.5 \times 29.75 + \frac{4 \times \pi \times 29.75^2}{2}) \div 4050000</math></p> <p>OR</p> <p>SC2 for an answer of 64(.1...) tins from <math>20000 \times (\pi \times 79.5 \times 29.75 + \frac{4 \times \pi \times 29.75^2}{2}) \div 4050000</math></p> <p>OR</p> <p>SC1 for a correct evaluation (rounded, truncated or unrounded) of the calculation <math>20000 \times (\pi \times 79.5 \times 29.75 + \frac{4 \times \pi \times 29.75^2}{2}) \div 4050000</math></p> <p>where <math>79 \leq \text{'their 79.5'} &lt; 80</math> and <math>29.5 \leq \text{'their 29.75'} &lt; 30</math> and <math>4000000 &lt; \text{'their 4 050 000'} \leq 4100000</math></p> <p>OR</p> <p>If no marks awarded,          SC1 for use of 80.5 and 30.25</p>
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<p>8(c) Statements required:</p> <ul style="list-style-type: none"> <li>• Number the parts from (0000)1 to 20000</li> <li>• Consider successive 5-digit numbers</li> <li>• Use numbers in the range e.g. Use numbers from (0000)1 to 20000 or Do not use 0000 or numbers &gt; 20000</li> <li>• Ignore repeats</li> </ul> <p>(Working in rows would give parts) (0)1325, 18266, <del>(0)1325</del>, (0)5929, 10429, (0)2891 OR</p> <p>(Working in columns would give parts) (0)5929, (0)1325, 10429, <del>(0)1325</del>, (0)2891, 18266</p>	<p>E2</p> <p>E1 for any 2 or 3 correct statements</p> <p>B1</p>	<p>All 4 needed for E2 E1 for any 2 or 3 correct statements</p> <p>Allow an equivalent numbering system e.g. (0000)0 to 19999 Their numbering system can be implied by the range of numbers they state they will choose from</p> <p>Allow the 2<sup>nd</sup> statement to be implied by their numbering of the parts (from 00001) AND their use of 5-digit numbers in their answer OR 5-digit numbers used in their answer and e.g. 01325 seen</p> <p>Do not allow 'Use numbers less than 20000' if they have numbered the parts from 00001 to 20000</p> <p>ISW. Part numbers can be given in any order</p>
<p><u>8(c) Alternative method:</u> Statements required:</p> <ul style="list-style-type: none"> <li>• Number the parts from (0000)1 to 20000</li> <li>• Consider successive 5-digit numbers</li> <li>• Divide each number by 20000 and use the remainder to choose a part</li> <li>• If the 5-digit number is 00000, then part 20000 is chosen, and ignore repeats.</li> </ul> <p>(Working in rows would give parts) (0)6923, (0)1325, 18552, <del>(0)6923</del>, (0)8925, 12712 OR</p> <p>(Working in columns would give parts) (0)6923, (0)8925, 15775, (0)5929, <del>(0)8925</del>, (0)1325</p>	<p>E2</p> <p>B1</p>	<p>All 4 needed for E2 E1 for any 2 or 3 correct statements</p> <p>Allow an equivalent numbering system e.g. (0000)0 to 19999 Their numbering system can be implied by the range of numbers they state they will choose from</p> <p>Allow the 2<sup>nd</sup> statement to be implied by their numbering of the parts (from 00001) AND their use of 5-digit numbers in their answer OR 5-digit numbers used in their answer and e.g. 06923 seen</p> <p>If (0000)0 to 19999 used, when the remainder is 0, part (0000)0 is selected</p> <p>ISW</p>

<p>15.</p> $23.5 - \frac{0.725}{8.35}$ $= 23.41$	<p>M2</p> <p>A1</p>	<p>If many attempts are offered without a method/answer being identified then mark final attempt.</p> <p>Accept 23.4999... or 8.34999... (or using recurring dot notation).</p> <p>Do <u>not</u> accept truncated values of 23.49 or 23.499 or 8.349 or 8.3499.</p> <p>Award M1 for correct use of values <math>23 &lt; b \leq 24</math>, <math>0.72 \leq c &lt; 0.73</math> and <math>8.3 &lt; d \leq 8.4</math></p> <p>OR award M1 for correct use of 2 of the 3 correct limits.</p> <p>Allow sight of 23.413(...) for M2.</p> <p>Only award A1 if M2 gained.</p>
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Unit 1: Higher Tier	Mark	Comments
1.(c) $4\frac{1}{2}$ or 4.5 or $\frac{9}{2}$	B3	<p>Mark final answer. Award B2 for an unsimplified evaluation as a single fraction or mixed number e.g.</p> <ul style="list-style-type: none"> <li>• <math>4\frac{7}{14}</math></li> <li>• <math>3\frac{21}{14}</math></li> <li>• <math>\frac{63}{14}</math></li> <li>• <math>\frac{441}{98}</math> or equivalent</li> <li>• <math>4 + \frac{1}{2}</math>.</li> </ul> <p>FT for one of the following:</p> <ul style="list-style-type: none"> <li>• adding 'their improper fractions' (which incorporate the entire numbers) provided fractions have a common denominator (one numerator must be correct) and answer given in a (proper or improper) simplified form</li> <li>• 3 + 'their fractions' evaluated correctly and in a simplified form, provided fractions have a common denominator (one numerator must be correct)</li> <li>• 'their 3' + 1.5 (or equivalent) in a simplified form</li> <li>• <math>3 + \frac{1}{2}</math> (or equivalent in its simplified form) evaluated provided <math>\frac{1}{2}</math> has come from two fractions with a common denominator (e.g. <math>\frac{10}{14} + \frac{11}{14} = \frac{21}{14} = 1\frac{7}{14} + 3 = 3\frac{1}{2}</math>).</li> </ul> <p>Award B1 for sight of two fractions with a common denominator (allow an error in one numerator) e.g.</p> <ul style="list-style-type: none"> <li>• <math>(1)\frac{10}{14} + (2)\frac{11}{14}</math></li> <li>• <math>\frac{24}{14} + \frac{39}{14}</math></li> <li>• <math>\frac{168}{98} + \frac{273}{98}</math> or equivalent.</li> </ul> <p>An unsupported answer of <math>4\frac{1}{2}</math> or 4.5 or <math>\frac{9}{2}</math> is awarded B3.</p>



Unit 2: Higher Tier	Mark	Comments
1(a) $(2.31 \div 7) \div 0.30$ or $(2.31 \div 0.30) \div 7$ or $(231 \div 7) \div 30$ or $(231 \div 30) \div 7$ or equivalent  1.1 (kWh)	M2          A1	Allow if brackets are implied in further working May be shown in stages  M1 for any of the following: <ul style="list-style-type: none"> <li>• <math>2.31 \div 0.30</math> (= 7.7)</li> <li>• <math>2.31 \div 7</math> (= 0.33)</li> <li>• <math>(231 \div 7) \div 30</math> (= 110)</li> <li>• <math>(2.31 \div 7) \div 30</math> (= 0.011)</li> <li>• <math>(231 \div 0.30) \div 7</math> (= 110)</li> <li>• <math>(2.31 \div 30) \div 7</math> (= 0.011)</li> </ul> CAO. Ignore incorrect units
1(b) (Height freezer door) $2 \times 1800 \div 5$ or $\frac{2}{5} \times 1800$ or $0.4 \times 1800$ or equivalent  720 (mm)  ((Diagonal of freezer door) <sup>2</sup> =) $600^2 + 720^2$  Diagonal <sup>2</sup> = 878 400 or (Diagonal =) $\sqrt{878\ 400}$  (Diagonal =) 937(.22... mm)	M1  A1  M1  A1  A1	Or alternative <b>full</b> method FT 'their height of freezer door' including 1080 or 1800 Accept working in m or cm for possible M1, A1  Final answer must be given in mm FT from M1 for the correctly evaluated square root of 'their 878 400' provided 'their answer' > 'their 720' for possible A1  If final M0 A0 A0 awarded as a different length, not 'their 720', is used to calculate the diagonal, award SC1 for a correct statement of Pythagoras' Theorem, and SC1 for a correct evaluation of 'their diagonal'

<p>3(a) (Length of the flagpole below the rod =)  <math>3.8 \times \sin 55^\circ</math> or <math>3.8 \times \cos (90^\circ - 55^\circ)</math>  or <math>380 \times \sin 55^\circ</math> or <math>380 \times \cos (90^\circ - 55^\circ)</math></p> <p style="text-align: center;">3.11(2...m) or 311(.2.. cm)</p> <p>(Total length <math>1.5 + 3.11 =</math>) 4.61 (m) or 461 (cm)</p>	<p>M2</p> <p>A1</p> <p>A1</p>	<p>Or alternative full method  M1 for correct working without isolating 'length'  <math>\sin 55^\circ = \frac{\text{length}}{3.8}</math> or <math>\cos (90^\circ - 55^\circ) = \frac{\text{length}}{3.8}</math>  or <math>\sin 55^\circ = \frac{\text{length}}{380}</math> or <math>\cos (90^\circ - 55^\circ) = \frac{\text{length}}{380}</math></p> <p>Allow 3.1 (m) or 310 (cm)</p> <p>Must be to the nearest cm  FT provided at least M1 previously awarded, i.e. for 1.5 + 'their 3(.).11' correctly evaluated, to nearest cm, <u>and</u> 'their 3.11' is to at least 2 decimal places</p> <p>If units are given they must be correct</p>
<p>3(b)(i) <math>120 \times 64 \div 80</math> or <math>64 \times 1.5</math> or <math>120 \times 0.8</math>  or <math>120 \div 1.25</math> or <math>64 \div \frac{2}{3}</math> or equivalent</p> <p style="text-align: center;">96 (cm)</p>	<p>M1</p> <p>A1</p>	<p>Answer space takes precedence</p>
<p>3(b)(ii) <math>75 \times 80 \div 120</math> or <math>75 \div 1.5</math> or <math>75 \times \frac{2}{3}</math>  or <math>80 \div 1.6</math> or <math>80 \times 0.625</math> or <math>64 \times 75 \div 96</math>  or equivalent</p> <p style="text-align: center;">50 (cm)</p>	<p>M1</p> <p>A1</p>	<p>FT from (b)(i) <math>64 \times 75 \div</math> 'their 96' or equivalent</p> <p>Answer space takes precedence</p>

<p>6.</p> <p>(Smallest possible area =)  <math>605 \times 295 - 105 \times 205 - 225 \times 145</math>                  or equivalent</p> <p>or <math>178475 - 21525 - 32625</math> or equivalent</p> <p>or <math>178475 - 54150</math></p> <p style="text-align: right;"><math>= 124325 \text{ (cm}^2\text{)}</math></p> <p>(Least number of litres Teifion could possibly use =)  <math>3 \times 124325 \div 55000</math>                  or <math>372975 \div 55000</math></p> <p style="text-align: right;"><math>= 6.78(13\dots)</math> or 6.8 (litres)</p>	<p>Accept use of upper bounds e.g. 104.999... with a clear recurring digit. <u>Do not accept use of e.g. 104.99</u></p> <p>M4 M3 for an appropriate calculation using 3 products with any 2 correct                  M2 for 'their <math>605 \times 295</math>' – 'their <math>105 \times 205</math>' – 'their <math>225 \times 145</math>' where  <math>600 \leq</math> 'their 605' <math>&lt; 610</math> and  <math>290 \leq</math> 'their 295' <math>&lt; 300</math> and  <math>100 &lt;</math> 'their 105' <math>\leq 110</math> and  <math>200 &lt;</math> 'their 205' <math>\leq 210</math> and  <math>140 &lt;</math> 'their 145' <math>\leq 150</math> and  <math>220 &lt;</math> 'their 225' <math>\leq 230</math></p> <p>M1 for use of <math>605 \times 295</math> OR <math>105 \times 205</math> OR <math>225 \times 145</math></p> <p>A1 CAO                  May be implied by <math>(3 \times 124325 =) 372975</math></p> <p>M1 FT 'their derived 124325'                  Allow M1 for <math>3 \times</math> 'their 124325' + 'their 55000' where <math>50000 &lt;</math> 'their 55000' <math>\leq 60000</math></p> <p>A1 Allow an answer of 6.7 or 7 from correct working                  On FT, accept rounding up to nearest whole number                  On FT, allow truncation to 1 d.p. or better</p> <p>If no marks awarded, and from a misinterpretation of the question,                  SC3 for an answer of 9.335 or 9.3 or 9.33 or 9.34 or 9.4 or 10 (litres) from  <math display="block">3 \times \frac{(615 \times 305 - 95 \times 195 - 215 \times 135)}{45000}</math>                 or <math display="block">\left[ \frac{3 \times (187575 - 18525 - 29025)}{45000} \right]</math></p> <p>OR</p> <p>SC2 for any one of the following:</p> <ul style="list-style-type: none"> <li> <math display="block">3 \times \frac{(615 \times 305 - 95 \times 195 - 215 \times 135)}{45000}</math>                     or <math display="block">\left[ \frac{3 \times (187575 - 18525 - 29025)}{45000} \right]</math>                     but not evaluated correctly                 </li> <li>                     correct evaluation (unrounded, rounded or truncated) from  <math>3 \times</math> ('their <math>615 \times 305</math>' – 'their <math>95 \times 195</math>' – 'their <math>215 \times 135</math>') + 'their 45000' where  <math>610 &lt;</math> 'their 615' <math>\leq 620</math> and  <math>300 &lt;</math> 'their 305' <math>\leq 310</math> and  <math>90 &lt;</math> 'their 95' <math>&lt; 100</math> and  <math>190 \leq</math> 'their 195' <math>&lt; 200</math> and  <math>210 \leq</math> 'their 215' <math>&lt; 220</math> and  <math>130 \leq</math> 'their 135' <math>&lt; 140</math> and  <math>40000 \leq</math> 'their 45000' <math>&lt; 50000</math> </li> </ul> <p>OR</p> <p>SC1 for <math>3 \times</math> ('their <math>615 \times 305</math>' – 'their <math>95 \times 195</math>' – 'their <math>215 \times 135</math>') + 'their 45000' using values in the same ranges as SC2, but not evaluated correctly</p>
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12. $\frac{1}{4} \times \frac{4}{3} \times \pi \times 7 \cdot 3^3$ OR $\frac{1}{3} \times \pi \times 7 \cdot 3^3$ (o.e.) = 407 (cm <sup>3</sup> )	M1 A2	May be seen in stages. Award A1 for sight of one of the following: <ul style="list-style-type: none"><li>• an answer 407 (cm<sup>3</sup>) followed by further incorrect rounding</li><li>• an answer in the range 407.17 (cm<sup>3</sup>) to 407.44(cm<sup>3</sup>)</li><li>• 129(.67...)π (cm<sup>3</sup>)</li><li>• 130π (cm<sup>3</sup>) from correct method/work seen.</li><li>• an answer 410 (cm<sup>3</sup>) from correct method/work seen</li><li>• an answer of 408(cm<sup>3</sup>) [from 1630÷4 to 3s.f.]</li><li>• an answer of 407·0(cm<sup>3</sup>).</li></ul> If no marks, award SC1 for sight of 1630(cm <sup>3</sup> ) [from evaluating $\frac{4}{3} \times \pi \times 7 \cdot 3^3$ to 3s.f.].
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**2. Marking Abbreviations**

The following may be used in marking schemes or in the marking of scripts to indicate reasons for the marks awarded.

cao = correct answer only

MR = misread

PA = premature approximation

bod = benefit of doubt

oe = or equivalent

si = seen or implied

ISW = ignore subsequent working

F.T. = follow through ( ✓ indicates correct working following an error and ✘ indicates a further error has been made)

Anything given in brackets in the marking scheme is expected but, not required, to gain credit.

**UNIT 1: NON-CALCULATOR, HIGHER TIER**

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GCSE Mathematics Unit 1 · Higher Tier	Mark	Comments
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*End of solutions*