

# REVISE

.wales

## F3.12 – Mean, modal class & median group from grouped data

*Mark schemes for the F3.12 question pack*

*Spec 4.2.9, 4.2.11, 4.2.13, 4.2.14, 4.2.15, 4.2.16 – Unit 3*

SOLUTIONS · 2025 SPECIFICATION

*Mark schemes for the 12 questions in the corresponding revise.wales question pack (35 marks total). Sources: legacy WJEC GCSE papers, WJEC SAM, and custom-authored mark schemes. Pack layout © revise.wales.*

<p>11.(a)</p> <table border="1" data-bbox="225 230 691 336"> <tr> <td>Throws</td> <td>20</td> <td>40</td> <td>60</td> <td>80</td> <td>100</td> </tr> <tr> <td>Heads</td> <td>11</td> <td>18</td> <td>24</td> <td>30</td> <td>37</td> </tr> <tr> <td>Rel. Fq.</td> <td>0.55</td> <td>0.45</td> <td>0.4</td> <td>0.375</td> <td>0.37</td> </tr> </table>	Throws	20	40	60	80	100	Heads	11	18	24	30	37	Rel. Fq.	0.55	0.45	0.4	0.375	0.37	<p>B1 B1</p>	
Throws	20	40	60	80	100															
Heads	11	18	24	30	37															
Rel. Fq.	0.55	0.45	0.4	0.375	0.37															
<p>11.(b) (Mid-points are) 4.5, 14.5 and 24.5.  (Estimated total =)  <math>3 \times 4.5 + 5 \times 14.5 + 2 \times 24.5</math> (= 135)  + 10  (Estimated mean =) = 13.5  (Difference = <math>15.2 - 13.5 =</math>) 1.7</p>	<p>B1 M1 m1 A1 B1</p>	<p>F.T. 'their mid-points' if within group. C.A.O. F.T. for difference between 15.2 and 'their derived estimated mean (<math>\neq 15.2</math>)'. Allow -1.7</p>																		

<p>10.(a) <math>\frac{1}{6} \times \frac{1}{4}</math> or equivalent <math>= \frac{1}{24}</math> ISW</p>	<p>M1 A1</p>	<p>Accept 0.0416... or 0.0417 or 0.042 for M1A1 M1A0 for '1 in 24', '1:24'.</p>																																																
<p>10.(b) <math>\frac{1}{5} + \frac{1}{10}</math> or equivalent. <math>= \frac{3}{10}</math> or equivalent. ISW</p>	<p>M1 A1</p>																																																	
<p>11. <math>(AC^2 =) 10 \cdot 8^2 + 14 \cdot 4^2</math> <math>AC^2 = 324</math> or <math>(AC =) \sqrt{324}</math> <math>(AC =) 18(\text{cm})</math></p> <p>(Area ACD =) <math>\frac{24 \times 18}{2}</math> <math>= 216 (\text{cm}^2)</math></p>	<p>M1 A1 A1      M1 A1</p>	<p>Accept equivalent of using cos rule (as <math>\cos 90 = 0</math>). F.T. <math>\sqrt{\text{their } 324}</math> provided M1 gained. Final answer of <math>AC = 324</math> is M1A0A0. <u>Alternative method to find AC</u> A correct and complete method (using two trigonometric relationships) M2 <math>AC = 18(\text{cm})</math> A1</p> <p>FT 'their stated AC'. (May be shown on the diagram) Accept equivalent of using <math>\frac{1}{2} \times 24 \times 18 \times \sin 90</math> (as <math>\sin 90 = 1</math>).</p>																																																
<p>12.</p> <p>One correct evaluation <math>7.2 \leq x \leq 7.3</math> 2 correct evaluations <math>7.275 \leq x \leq 7.295</math>, one <math>&lt; 0</math>, one <math>&gt; 0</math>. 2 correct evaluations <math>7.275 \leq x \leq 7.285</math>, one <math>&lt; 0</math>, one <math>&gt; 0</math>.</p> <p><math>x = 7.28</math></p>	<p>B1 B1 M1 A1</p>	<p>Correct evaluation regarded as enough to identify if negative or positive. If evaluations not seen accept 'too high' or 'too low'. Look out for equating <math>x^3 - 5x = 350</math></p> <table border="0"> <tr> <td><math>x</math></td> <td><math>x^3 - 5x - 350</math></td> <td></td> <td></td> </tr> <tr> <td>7.2</td> <td>-12.75(2)</td> <td></td> <td></td> </tr> <tr> <td>7.21</td> <td>-11(-2..)</td> <td></td> <td></td> </tr> <tr> <td>7.22</td> <td>-9(-7...)</td> <td></td> <td></td> </tr> <tr> <td>7.23</td> <td>-8(-2...)</td> <td></td> <td></td> </tr> <tr> <td>7.24</td> <td>-6(-6...)</td> <td></td> <td></td> </tr> <tr> <td>7.25</td> <td>-5(-1...)</td> <td></td> <td></td> </tr> <tr> <td>7.26</td> <td>-3(-6...)</td> <td>7.275</td> <td>-1(-3....)</td> </tr> <tr> <td>7.27</td> <td>-2(-1...)</td> <td>7.284</td> <td>0(-04..)</td> </tr> <tr> <td><b>7.28</b></td> <td><b>-0.5(7..)</b></td> <td><b>7.285</b></td> <td><b>0.1(9..)</b></td> </tr> <tr> <td><b>7.29</b></td> <td><b>0.9(7..)</b></td> <td>7.295</td> <td>1(-7....)</td> </tr> <tr> <td>7.3</td> <td>2.5(17)</td> <td></td> <td></td> </tr> </table>	$x$	$x^3 - 5x - 350$			7.2	-12.75(2)			7.21	-11(-2..)			7.22	-9(-7...)			7.23	-8(-2...)			7.24	-6(-6...)			7.25	-5(-1...)			7.26	-3(-6...)	7.275	-1(-3....)	7.27	-2(-1...)	7.284	0(-04..)	<b>7.28</b>	<b>-0.5(7..)</b>	<b>7.285</b>	<b>0.1(9..)</b>	<b>7.29</b>	<b>0.9(7..)</b>	7.295	1(-7....)	7.3	2.5(17)		
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<p>14. (Mid-points) 2.5, (7.5), 12.5 and 17.5. <math>8 \times 2.5 + (0 \times 7.5) + 7 \times 12.5 + 5 \times 17.5</math> <math>(20 + 0 + 87.5 + 87.5 = 195)</math></p> <p><math>\div 20</math> <math>= 9.75</math></p>	<p>B1 M1  m1 A1</p>	<p>Allow for sight of mid-points. F.T. 'their mid-points' including bounds, provided they fall within the classes (including lower and upper bounds and used consistently). C.A.O.</p>																																																
<p>15. (<math>x =</math>) <math>\frac{360}{15}</math> or <math>180 - \frac{(15-2) \times 180}{15}</math> or equivalent <math>= 24(^{\circ})</math></p> <p>(BR =) <math>8 \times \cos 24</math> or <math>8 \times \sin (90 - 24)</math></p> <p><math>= 7.3(0...)(\text{cm})</math> or <math>7.31(\text{cm})</math></p>	<p>M1  A1 M2  A1</p>	<p>May be seen in parts.</p> <p>FT 'their stated value for <math>x</math>' (<math>x &lt; 90^{\circ}</math>) M1 for <math>\frac{BR}{8} = \cos 24</math> or <math>\frac{BR}{8} = \sin (90 - 24)</math> Accept equivalent of using sin rule (as <math>\sin 90 = 1</math>). <u>Alternative method to find BR</u> A correct and complete method (using two trigonometric relationships and possibly Pythagoras's theorem) M2 <math>BR = 7.3(0...)(\text{cm})</math> or <math>7.31(\text{cm})</math> A1</p>																																																

**WJEC GCSE MATHEMATICS**  
**AUTUMN 2021 MARK SCHEME**

Unit 2: Intermediate Tier	Mark	Comments
1.(a) $7x = 14$ $x = 2$	B1 B1	FT from $7x = k$ . Accept $x = k/7$ (but, if on FT $k$ is a multiple of 7, final answer must be given as a whole number.) B1B0 for ' $x = 14/7$ '  An evaluated FT for $k \div 7$ must be rounded or truncated to at least 2dp. e.g. $7x = 8$ (B0) followed by, $x = 8 \div 7$ (B0) $x = 8/7$ (B1), $x = 1\frac{1}{7}$ (B1), $x = 1.14$ (B1), $x = 1.1$ (B0)  Mark final answer. Allow 2 marks for embedded answer BUT only 1 mark if contradicted by $x \neq 2$ .
1.(b) 10	B2	C.A.O. B1 for sight of 17.4 OR -7.4 Do not accept 17.4f nor -7.4g Do <u>not</u> treat the use of 3.7 for -3.7 as a misread.
2.(a) $\frac{24}{54}$	B1	
2.(b) 23	B1	
2.(c) 1853	B1	
3. (Total number of paper clips =) $200 \times 440 \times n$ where $320 \leq n \leq 330$ .  Correct evaluation.  (To the nearest ten million) 30 000 000 (paper clips)	M2  A1  B1	M1 for $200 \times n$ OR $440 \times n$ where $320 \leq n \leq 330$ . Allow use of 400 or 450 for 440. <u>Note</u> If $n$ taken to be 225 or 425 treat as a misread and allow M2 but penalise -1 from any further A1, B1 marks gained. A1 CAO from their numbers if M2 gained. ( $n=320$ gives 28 160 000, $n=325$ gives 28 600 000, $n=330$ gives 29 040 000.) B1 FT 'their evaluation' if greater than 5 million. A final answer of 30 million implies M2A1B1. Allow M2A0B0 for an unsupported final answer of 28 000 000 or 29 000 000.
OCW Organisation and Communication.          Accuracy of writing.	OC1          W1	For OC1, candidates will be expected to: <ul style="list-style-type: none"> <li>present their response in a structured way</li> <li>explain to the reader what they are doing at each step of their response</li> <li>lay out their explanation and working in a way that is clear and logical</li> <li>write a conclusion that draws together their results and explains what their answer means</li> </ul> For W1, candidates will be expected to: <ul style="list-style-type: none"> <li>show all their working</li> <li>make few, if any, errors in spelling, punctuation and grammar</li> <li>use correct mathematical form in their working</li> <li>use appropriate terminology, units, etc</li> </ul>
4.(a) 3	B1	If no answer seen, check table.
4.(b) 15	B1	If no answer seen, check table.

10. (-2, 1)	B2	B1 for: <ul style="list-style-type: none"> <li>one correct coordinate, or</li> <li>a clear indication of the correct position of the midpoint, or</li> <li>the correct coordinates reversed.</li> </ul>
11.(a) $7x = 14$ $x = 2$	B1 B1	FT from $7x = k$ . Accept $x = k/7$ (but, if on FT $k$ is a multiple of 7, final answer must be given as a whole number.) B1B0 for ' $x = 14/7$ '  An evaluated FT for $k \div 7$ must be rounded or truncated to at least 2dp. e.g. $7x = 8$ (B0) followed by, $x = 8 \div 7$ (B0) $x = 8/7$ (B1), $x = 1\frac{1}{7}$ (B1), $x = 1.14$ (B1), $x = 1.1$ (B0)  Mark final answer. Allow 2 marks for embedded answer BUT only 1 mark if contradicted by $x \neq 2$ .
W Accuracy of writing.	W1	For W1, candidates will be expected to: <ul style="list-style-type: none"> <li>show all their working</li> <li>make few, if any, errors in spelling, punctuation and grammar</li> <li>use correct mathematical form in their working</li> <li>use appropriate terminology, units, etc</li> </ul>
11.(b) 10	B2	C.A.O. B1 for sight of 17.4 OR -7.4 Do not accept 17.4f nor -7.4g Do not treat the use of 3.7 for -3.7 as a misread.
12. (Total number of paper clips =) $200 \times 440 \times n$ where $320 \leq n \leq 330$ .  Correct evaluation.  (To the nearest ten million) 30 000 000 (paper clips)	M2  A1  B1	M1 for $200 \times n$ OR $440 \times n$ where $320 \leq n \leq 330$ . Allow use of 400 or 450 for 440. <u>Note</u> If $n$ taken to be 225 or 425 treat as a misread and allow M2 but penalise -1 from any further A1, B1 marks gained. CAO from their numbers if M2 gained. ( $n=320$ gives 28 160 000, $n=325$ gives 28 600 000, $n=330$ gives 29 040 000.) FT 'their evaluation' if greater than 5 million. A final answer of 30 million implies M2A1B1. Allow M2A0B0 for an unsupported final answer of 28 000 000 or 29 000 000.
13.(a) 3	B1	If no answer seen, check table.
13.(b) 15	B1	If no answer seen, check table.
14.(a) (0)7:45 23 (March)	B2	B1 for each. B0 for (0)7:45 p.m.
14.(b) Sight of 5 miles $\equiv$ 8 km or equivalent.  Shows 15 miles to be 24 km AND a valid statement e.g. 'yes (it's nearly 25 km)', 'no (it's only 24 km)'. <u>Alternative method</u> Sight of 8 km $\equiv$ 5 miles or equivalent.  Shows 25 km to be 15.625 miles AND a valid statement e.g. 'yes (it's just over 15 miles)', 'no (it's over 15 miles)'.	B1  B1  B1  B1	Allow a more accurate conversion (5 miles $\equiv$ 8 to 8.05 km). Do not accept 3 miles $\equiv$ 5 km '15 miles is 24 km' with no statement is B1B0. Accept a one word decision of 'Yes' or 'No' as a statement.  Allow a more accurate conversion (8 km $\equiv$ 4.97 to 5 miles). Do not accept 5 km $\equiv$ 3 miles '25 km is 15.625 miles' with no statement is B1B0. Accept a one word decision of 'Yes' or 'No' as a statement.

6(a) (Direct <sup>2</sup> =) $200^2 + 350^2$ Direct <sup>2</sup> = 162500 or (Direct =) $\sqrt{162500}$	M1 A1	
(Direct =) $403(.11\dots \text{ m})$ or $50\sqrt{65} \text{ (m)}$ or $\sqrt{162500} \text{ (m)}$	A1	FT from M1 for the correctly evaluated square root of 'their 162500' provided 'their answer' > 350 (m) May be implied in further working Mark final answer or the answer they go on to use, but then FT
(Extra distance =) $200 + 350 - 403(.1\dots)$ or $200 + 350 - 50\sqrt{65}$ or $200 + 350 - \sqrt{162500}$	M1	FT 'their derived $403(.11\dots)$ ' > 350 and from an attempt to use Pythagoras' Theorem
$146.8(87\dots\text{m})$ or $146.9(\text{m})$ or $147(\text{m})$	A1	

<p>6(b)(i) Selects or unambiguously implies 'No' with a reason, e.g.                  'the median is in group &gt;200m to 1000m (and he lives 200m away)',                  'median is more than 200m away (but Ronnie is 200m away)'</p>	<p>E1</p>	<p>Needs to compare 200(m) with median &gt;200(m)                  The 200(m) can be implied from selecting 'No'</p> <p>Ignore additional spurious statements</p> <p>Allow 'No' with a reason, e.g.                  'Ronnie's distance is in the first group, the median is in the second group'                  'Ronnie only travels 200m which is less than the median (distance)'                  'because the median distance travelled is between 200m and 1000m'                  'Ronnie doesn't travel the distance of the 17.5(th) person'                  'Ronnie doesn't travel the distance of the 17(th) (or 18<sup>th</sup>) person'                  'the median 17.5(th)'                  'the median 17(th) (or 18(th))'                  'he only walks 200m when the (median) distance is higher'                  'he only walks 200m which is less than the median'                  'can't estimate exact number from the group  <math>200 &lt; d \leq 1000</math>                  'the median could be 880'                  '9 less than half of 35'                  '26 students walk further than him'</p> <p>Do not accept 'No' with a reason e.g.                  'Ronnie's distance is in the first group'                  'the median is 250m'</p>														
<p>6(b)(ii) Midpoints 150, 600, 2000, 5000</p> $150 \times 9 + 600 \times 10 + 2000 \times 15 + 5000 \times 1$ <p>(= 1350 + 6000 + 30000 + 5000 = 42350 m)</p> <p style="text-align: right;">÷ 35</p> <p style="text-align: right;">1210 (m)</p>	<p>B1</p> <p>M1</p> <p>m1</p> <p>A1</p>	<p>Check the table                  Sight of 7750 implies correct midpoints</p> <p>FT 'their midpoints' provided at least 3 are within or at the bounds of the appropriate groups</p> <p>Answer space takes precedence</p>														
<p>6(c) <math>(140 \div 7 =) 20</math>                  or <math>140 \div 20 = 7</math> or <math>7 \times 20 = 140</math></p> <table border="1" data-bbox="172 1406 576 1458"> <tr> <td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td> </tr> <tr> <td>2</td><td>22</td><td>42</td><td>62</td><td>82</td><td>102</td><td>122</td> </tr> </table>	1	2	3	4	5	6	7	2	22	42	62	82	102	122	<p>B1</p> <p>B1</p>	<p>May be implied by any of the following:</p> <ul style="list-style-type: none"> <li>consistent position patterns + 20 indicated for at least 4 consecutive positions e.g. (2,) 20, 40, 60, 80, 100, 120</li> <li>sight of 22 for student 2 with no further working or entries</li> </ul> <p>CAO</p>
1	2	3	4	5	6	7										
2	22	42	62	82	102	122										

<p>6(a)(i) Unambiguously indicates or states 'Yes' with a reason, e.g.          'both 25 kg to 35 kg',          'the highest frequencies at the same mass'</p>	E1	<p><i>Ignore any additional spurious or contradictory statements provided 'Yes' selected</i></p> <p>Allow 'Yes' with a reason, e.g.          'both at 30 kg',          'both at the same mass',          'both have the same mass',          'tallest (highest frequency) is 30kg for both polygons'</p> <p>Do not accept 'Yes' with a reason, e.g.          'don't know',          'both in the same place',          'the groups have the same width',          'the graph tells us this'</p>
<p>6(a)(ii) Unambiguously indicates or states 'Can't tell' with a reason, e.g.          'there were 30 dogs with a masses between 15kg and 25kg',          'no raw data is given',          'the actual mass of each dog is not given',          'the data is grouped'</p>	E1	<p><i>Ignore any additional spurious or contradictory statements provided 'Can't tell' selected</i></p> <p>Allow 'Can't tell' with a reason, e.g.          'doesn't show this',          'you can't tell the exact number of dogs'          'doesn't give the amount of dogs'</p> <p>Do not accept 'Can't tell' with a reason, e.g.          'don't know',          'it is an estimate',          'it isn't accurate',          'because they can be anywhere from 10kg to 20kg'</p>
<p>6(a)(iii) Unambiguously indicates or states 'Correct' with a reason, e.g.          'Pencwm polygon shows a greater drop for greater masses',          'fewer dogs but more large dogs in Glanafon',          'more dogs in Pencwm, but fewer large dogs',          'about the same number of large dogs, with fewer dogs in Glanafon',          'about the same number of large dogs, with more dogs in Pencwm',</p>	E1	<p><i>Ignore any additional spurious or contradictory statements provided 'Correct' selected</i></p> <p><b>Do not</b> allow a reason based on calculations of proportions <b>alone</b>, e.g. Pencwm 27.5%, Glanafon 41.6%</p> <p>Allow 'Correct' with a reason, e.g.          'Pencwm (polygon) shows a steeper drop from 30 kg',          'line for Pencwm is steeper (drop)',          'Glanafon (polygon) has a less steep drop for larger dogs',          'the greater masses are more frequent (in Glanafon)',          '2 of the 3 points for Glanafon are above Pencwm',          'Pencwm line drops below Glanafon after 40 (kg)'</p> <p>Do not accept 'Correct' with a reason, e.g.          '36 dogs in Pencwm and 37 dogs in Glanafon' alone without considering proportion,          'the greatest is 45 kg',          'higher frequency in Glanafon',          'Pencwm is bigger but doesn't have higher proportion'          'as seen by the skew in (the) Glanafon (polygon)',          'seen by the shape (of the polygon) for Glanafon'</p>

<p>6(b) (Total number of dogs  <math>20 + 30 + 45 + 25 + 7 + 4 =</math> 131</p> <p><math>10 \times 20 + 20 \times 30 + 30 \times 45 + 40 \times 25 + 50 \times 7 + 60 \times 4</math>  <math>(= 200 + 600 + 1350 + 1000 + 350 + 240)</math>  <math>(= 3740)</math></p> <p style="text-align: right;"><math>+ 131</math></p> <p>(28.5(496.... kg) so)      3.95 (kg) (less)</p>	<p>B1    May be implied by the sight of  <math>((20 + 30 + 45 + 25 + 7 + 4) \div 6 =) 21.8(33\dots)</math></p> <p>M1    Ignore any additional products seen                      FT 'their midpoints' provided at least 5 are within or at the bounds of the relevant groups                      e.g. use of</p> <ul style="list-style-type: none"> <li>• lower bounds of each group gives 3085</li> <li>• upper bounds of each group gives 4395</li> </ul> <p>m1    FT an error in summing 20, 30, 45, 25, 7 and 4</p> <p>A2    CAO                      ISW further rounding or truncation                      Allow 4 (kg) from correct working                      Accept (29 (kg) and) 3.5 (kg) from correct working</p> <p>Award A1 for any of the following as the final answer</p> <ul style="list-style-type: none"> <li>• 28.5(496.... kg)</li> <li>• 29 (kg) (from correct working)</li> </ul> <p>OR</p> <p>Award A1 on FT from M1 m1 previously awarded for a correct evaluation of 'their estimate mean' e.g. use of lower bounds gives <math>(3085/131 =) 23.54\dots</math></p>
<p><u>6(b) Alternative MS if Glanafon's last 2 points used for possible award of B1 M1 m1 only</u>                      (Sight of <math>20 + 30 + 45 + 25 + 10 + 7 =</math>) 137</p> <p><math>10 \times 20 + 20 \times 30 + 30 \times 45 + 40 \times 25 + 50 \times 10 + 60 \times 7</math>  <math>(= 200 + 600 + 1350 + 1000 + 500 + 420)</math>  <math>(= 4070)</math></p> <p style="text-align: right;"><math>+ 137</math></p>	<p>B1    May be implied by the sight of  <math>((20 + 30 + 45 + 25 + 10 + 7) \div 6 =) 22.8(33\dots)</math></p> <p>M1    Ignore any additional products seen                      FT 'their midpoints' provided at least 5 are within or at the bounds of the relevant groups                      e.g. use of</p> <ul style="list-style-type: none"> <li>• lower bounds of each group gives 3385</li> <li>• upper bounds of each group gives 4755</li> </ul> <p>m1    FT an error in summing 20, 30, 45, 25, 10 and 7</p>

Unit 2: Intermediate tier	Mark	Comments
6(a)(i) 18 to 24 hours	B1	
6(a)(ii) 97	B1	
6(a)(iii) 13	B1	
6(a)(iv) States or unambiguously implies 'No' with a reason, e.g. 'no people in group 0 to 6 hours'	E1	<p>Allow 'No' with e.g. 'the point before 6 hours is at zero'</p> <p>Do not allow 'Can't tell' with e.g. 'it is grouped data'</p> <p>Do not accept 'No' with e.g. 'it is grouped data' (unless explaining why)</p> <p>'there is no point at 6'</p> <p>'6 hours has a frequency of 0'</p> <p>'it does not match a group of people'</p> <p>'the first point is at 0 and the second one is at 20'</p> <p>'the first plot is at 20'</p> <p>'the first plot is at 9 hours'</p> <p>'the first plot above 0 is at 9 hours'</p> <p>'there is no information at 6 hours, it starts at 9 hours'</p> <p>'the shortest time is 9 hours'</p>
<p>6(b) Sight of 22.5, 25.5, 29.5 and 31.5 (mm)</p> <p>22.5 + 25.5 + 29.5 + 31.5 or 22+25+29+31 + 4 × 0.5 or equivalent</p> <p>109 (mm)</p>	<p>B1</p> <p>M1</p> <p>A1</p>	<p>Award B1 for sight of <math>4 \times 0.5</math> in an appropriate calculation</p> <p>Allow 0.4999(...) for 0.5, must clearly be a recurring 9 digit</p> <p>If B0, FT provided unambiguously chosen:  <math>22 &lt; \text{'their 22.5'} \leq 23</math>, <math>25 &lt; \text{'their 25.5'} \leq 26</math>,  <math>29 &lt; \text{'their 29.5'} \leq 30</math>, and <math>31 &lt; \text{'their 31.5'} \leq 32</math>,</p> <p>CAO. Ignore incorrect units given</p> <p>Ignore any working for least possible thickness also given, e.g. <math>21.5 + 22.5 + 28.5 + 30.5 = 105</math></p>

<p>8(a) Midpoints 1, 4, 7, 11, 16</p> $1 \times 8 + 4 \times 12 + 7 \times 20 + 11 \times 4 + 16 \times 6$ $= 8 + 48 + 140 + 44 + 96$ $= 336$ $+ 50$ $6.72 \text{ or } 6.7 \text{ (walks)}$	<p>B1</p> <p>M1</p> <p>m1</p> <p>A1</p>	<p>FT 'their midpoints' provided at least 4 lie within the appropriate group, including bounds throughout</p> <p>Use of lower bounds gives 276</p> <p>Use of upper bounds gives 396</p> <p>Allow rounded to 7 (walks) from appropriate working</p> <p>Use of lower bounds gives 5.5(2 walks) or 6 (walks)</p> <p>Use of upper bounds gives 7.9(2 walks) or 8 (walks)</p>
<p>8(b) 06(:)53 or 6(:)53 a.m.</p>	<p>B1</p>	<p>Allow 06(:)53 a.m. or 6(:)53</p> <p>Do not accept (0)6(:)53 p.m.</p>

Unit 2: Intermediate Tier	Mark	Comments
8(c) $(\text{Height})^2 = 7.6^2 - (18.8 - 12.6)^2$ or $(\text{Height})^2 = 7.6^2 - 6.2^2$  or $\cos^{-1}\left(\frac{18.8-12.6}{7.6}\right) = 35(.3345\dots)^\circ$ and $\sin 35(.33\dots)^\circ = \frac{\text{Height}}{7.6}$ or $\tan 35(.33\dots)^\circ = \frac{\text{Height}}{6.2}$  $\text{Height}^2 = 19.32$ or $(\text{Height} = ) \sqrt{19.32}$ or $(\text{Height} = ) 7.6 \times \sin 35(.33\dots)^\circ$ or $(\text{Height} = ) 6.2 \times \tan 35(.33\dots)^\circ$  $(\text{Height} = ) 4.39(54\dots \text{m})$ or $4.4(\text{m})$  (Volume of concrete) $\frac{1}{2} \times (12.6 + 18.8) \times 4.4 \times 50$ or $\frac{1}{2} \times 31.4 \times 4.4 \times 50$ or $\frac{1}{2} \times (18.8 - 12.6) \times 4.4 \times 50 + 12.6 \times 4.4 \times 50$ or $\frac{1}{2} \times 6.2 \times 4.4 \times 50 + 12.6 \times 4.4 \times 50$	M2	M1 for sight of $18.8 - 12.6$ with <ul style="list-style-type: none"> <li>any attempt to use Pythagoras' Theorem (including summing rather than subtraction)</li> <li><math>\cos^{-1}\left(\frac{18.8-12.6}{7.6}\right) = 35(.33\dots)^\circ</math> and an attempt to use sine or tan</li> </ul>
	A1	
	A1	Do not allow 4.3(m) from premature rounding of $35.3345\dots^\circ$ May be implied in further working Provided at least M2 previously awarded, FT from $\sqrt{\text{their } 19.32}$ provided $< 7.6$ (m)
	M2	FT 'their derived 4.4' provided <ul style="list-style-type: none"> <li>'their derived 4.4' <math>&lt; 7.6</math></li> <li>'their derived 4.4' <math>\neq 6.2</math></li> <li>'their derived 4.4' <math>\neq</math> 'their <math>18.8 - 12.6</math>'</li> </ul> May be seen in stages, e.g. with 'x 50' in further working  M1 for any one of the following: (Area of cross-section) <ul style="list-style-type: none"> <li><math>\frac{1}{2} \times (12.6 + 18.8) \times 4.4</math> (= 69.08 or 69.1m<sup>2</sup>)</li> <li><math>\frac{1}{2} \times (18.8 - 12.6) \times 4.4 + 12.6 \times 4.4</math> (= 13.64m<sup>2</sup> + 55.44m<sup>2</sup>)</li> </ul> (Volume cuboid) <ul style="list-style-type: none"> <li><math>12.6 \times 4.4 \times 50</math> (= 55.44 <math>\times</math> 50 = 2772 m<sup>3</sup>)</li> </ul> (Volume triangular prism) <ul style="list-style-type: none"> <li><math>\frac{1}{2} \times (18.8 - 12.6) \times 4.4 \times 50</math> (= 13.64 <math>\times</math> 50 = 682 m<sup>3</sup>)</li> </ul>
(Volume of concrete) Answer in the range 3450 (m <sup>3</sup> ) to 3455 (m <sup>3</sup> )	A1	FT from previous M2 only and 'their derived 4.4' from an attempt to use Pythagoras' Theorem or cosine followed by sine or tan  On FT from M2, allow a similar range from rounding or truncation  If previous M0 A0, award SC1 for an answer of 4867 (m <sup>3</sup> ) from 'their 4.4' = 6.2

<p>4(a) <math>20 \leq \text{time in minutes} &lt; 30</math></p>	<p>B1</p>	<p>Allow e.g.                  '20 to 30'                  '20 – 30'                  '20 &lt; time &lt; 30'                  '20 ≤ time ≤ 30'                  '20 &lt; time ≤ 30'                  '12 pupils for 20 to 30 minutes' (implies the group)                  '12 pupils in 20 – 30 minutes' (implies the group)                  '12 (pupils), 20 – 30 minutes' (2 answers side by side, mark the right-hand attempt)                  Sight of 20 and 30 with incorrect inequality signs, e.g. '20 ≤ 30'</p> <p>Do not accept, e.g.                  '12'                  '25'                  '20 – 30 minutes, 12 (pupils)', (as a choice of answers, mark the right-hand attempt)</p>
<p>4(b) 15</p>	<p>B1</p>	
<p>4(c) Unambiguously indicates 'Can't tell' with a reason, e.g.                  'doesn't give the raw data (for the group 0 to 10 minutes)',                  'only know (frequency) for the group 0 to (less than) 10 minutes'                  '5 pupils spent less than 10 minutes, but the diagram doesn't show if any of these spent no time'                  'it doesn't tell you exactly how many minutes each pupil spent individually'</p>	<p>E1</p>	<p>Allow 'Can't tell' with a reason such as, e.g.                  'grouped data',                  'data is grouped'                  'it is given in a range on the diagram'                  'it doesn't show specifically'                  'graph is not specific'                  'it doesn't give an exact time'                  'the graph gives 0 to 10 minutes making it impossible to get an accurate reading'                  'could be 1 minute each or 5 minutes each we don't know' (examples all within the group <math>0 \leq \text{time} &lt; 10</math>)                  'doesn't give the data for 0 minutes'                  'because the group is from greater than or <u>equal to</u> 0 minutes to less than 10 minutes'                  'graph does not say they did or not'                  'we can't see this on the diagram'                  'does not give enough data'</p> <p>Do not accept reasons that imply 0 minutes is not included in the diagram</p> <p>Do not accept, 'Can't tell' e.g.                  'the groups are an estimate'                  'could be 5 minutes each or 20 minutes each we don't know' (examples not all within the required group)                  'because the group is from <u>greater than</u> 0 minutes to less than 10 minutes'                  'doesn't tell us how many people there are'</p>

4(d) Unambiguously indicates 'No' with a reason, e.g.  
'it is the same number (both 5 pupils) but different  
number of Year 9 asked to Year 10',  
'the totals are different',  
'Year 9 percentage is lower (than Year 10)',  
'5/34 is not the same (percentage) as 5/33',  
'there are more pupils in Year 9 (than in Year 10)',  
'there are fewer pupils in Year 10 (than Year 9)'

E1

Check diagram for totals

If 'totals are different' is stated or clearly implied,  
ignore any incorrect totals or fractions given, provided  
the numerator of 5 pupils is correct

Allow 'No' with a reason, e.g.

'the difference is 1'

OR

Allow 'No' with sight of total 34 for Year 9 and 33 for  
Year 10

Do not accept, e.g.

'because the results are different'

'the difference is 2'

'there are more pupils in Year 10 (than in Year 9)',

unless the correct totals are seen

'there are fewer Year 9 (than Year 10)',

unless the correct totals are seen

7(a) $20 \leq \text{time in minutes} < 30$	B1	Allow e.g. '20 to 30' '20 – 30' '20 < time < 30' '20 ≤ time ≤ 30' '20 < time ≤ 30' '12 pupils for 20 to 30 minutes' (implies the group) '12 pupils in 20 – 30 minutes' (implies the group) '12 (pupils), 20 – 30 minutes' (2 answers side by side, mark the right-hand attempt) Sight of 20 and 30 with incorrect inequality signs, e.g. '20 ≤ 30'  Do not accept, e.g. '12' '25' '20 – 30 minutes, 12 (pupils)', (as a choice of answers, mark the right-hand attempt)
7(b) 15	B1	

<p>7(c) Unambiguously indicates 'Can't tell' with a reason, e.g.                  'doesn't give the raw data (for the group 0 to 10 minutes)',                  'only know (frequency ) for the group 0 to (less than) 10 minutes'                  '5 pupils spent less than 10 minutes, but the diagram doesn't show if any of these spent no time'                  'it doesn't tell you exactly how many minutes each pupil spent individually'</p>	<p>E1</p>	<p>Allow 'Can't tell' with a reason such as, e.g.                  'grouped data',                  'data is grouped'                  'it is given in a range on the diagram'                  'it doesn't show specifically'                  'graph is not specific'                  'it doesn't given an exact time'                  'the graph gives 0 to 10 minutes making it impossible to get an accurate reading'                  'could be 1 minute each or 5 minutes each we don't know' (examples all within the group <math>0 \leq \text{time} &lt; 10</math>)                  'doesn't give the data for 0 minutes'                  'because the group is from greater than or <u>equal to</u> 0 minutes to less than 10 minutes'                  'graph does not say they did or not'                  'we can't see this on the diagram'                  'does not give enough data'</p> <p>Do not accept reasons that imply 0 minutes is not included in the diagram</p> <p>Do not accept, 'Can't tell' e.g.                  'the groups are an estimate'                  'could be 5 minutes each or 20 minutes each we don't know' (examples not all within the required group)                  'because the group is from <u>greater than</u> 0 minutes to less than 10 minutes'                  'doesn't tell us how many people there are'</p>
<p>7(d) Unambiguously indicates 'No' with a reason, e.g.                  'it is the same number (both 5 pupils) but different number of Year 9 asked to Year 10',                  'the totals are different',                  'Year 9 percentage is lower (than Year 10)'                  '5/34 is not the same (percentage) as 5/33'                  'there are more pupils in Year 9 (than in Year 10)'                  'there are fewer pupils in Year 10 (than Year 9)'</p>	<p>E1</p>	<p>Check diagram for totals</p> <p>If 'totals are different' is stated or clearly implied, ignore any incorrect totals or fractions given, provided the numerator of 5 pupils is correct</p> <p>Allow 'No' with a reason, e.g.                  'the difference is 1'                  OR                  Allow 'No' with sight of total 34 for Year 9 <u>and</u> 33 for Year 10</p> <p>Do not accept, e.g.                  'because the results are different'                  'the difference is 2'                  'there are more pupils in Year 10 (than in Year 9)', unless the correct totals are seen                  'there are fewer Year 9 (than Year 10)', unless the correct totals are seen</p>

<p>9(a) (Length of the flagpole below the rod =)</p> $3.8 \times \sin 55^\circ \quad \text{or} \quad 3.8 \times \cos (90^\circ - 55^\circ)$ $\text{or } 380 \times \sin 55^\circ \quad \text{or} \quad 380 \times \cos (90^\circ - 55^\circ)$ <p style="text-align: center;">3.11(2...m) or 311(.2.. cm)</p> <p>(Total length 1.5 + 3.11 =) 4.61 (m) or 461 (cm)</p>	<p>M2</p> <p>A1</p> <p>A1</p>	<p>Or alternative full method</p> <p>M1 for correct working without isolating 'length'</p> $\sin 55^\circ = \frac{\text{length}}{3.8} \quad \text{or} \quad \cos (90^\circ - 55^\circ) = \frac{\text{length}}{3.8}$ $\text{or } \sin 55^\circ = \frac{\text{length}}{380} \quad \text{or} \quad \cos (90^\circ - 55^\circ) = \frac{\text{length}}{380}$ <p>Allow 3.1 (m) or 310 (cm)</p> <p>Must be to the nearest cm</p> <p>FT provided at least M1 previously awarded, i.e. for 1.5 + 'their 3(.11)' correctly evaluated, to nearest cm, <u>and</u> 'their 3.11' is to at least 2 decimal places</p> <p>If units are given they must be correct</p>
<p>9(b)(i) <math>120 \times 64 \div 80</math> or <math>64 \times 1.5</math> or <math>120 \times 0.8</math></p> <p>or <math>120 \div 1.25</math> or <math>64 \div \frac{2}{3}</math> or equivalent</p> <p style="text-align: center;">96 (cm)</p>	<p>M1</p> <p>A1</p>	<p>Answer space takes precedence</p>
<p>9(b)(ii) <math>75 \times 80 \div 120</math> or <math>75 \div 1.5</math> or <math>75 \times \frac{2}{3}</math></p> <p>or <math>80 \div 1.6</math> or <math>80 \times 0.625</math> or <math>64 \times 75 \div 96</math></p> <p>or equivalent</p> <p style="text-align: center;">50 (cm)</p>	<p>M1</p> <p>A1</p>	<p>FT from (b)(i) <math>64 \times 75 \div</math> 'their 96' or equivalent</p> <p>Answer space takes precedence</p>

*End of solutions*