

REVISE

.wales

F3.11 – Mean, median, mode & range – lists & ungrouped data

Mark schemes for the F3.11 question pack

Spec 4.2.8, 4.2.10 – Unit 3

SOLUTIONS · 2025 SPECIFICATION

Mark schemes for the 35 questions in the corresponding revise.wales question pack (90 marks total). Sources: legacy WJEC GCSE papers, WJEC SAM, and custom-authored mark schemes. Pack layout © revise.wales.

<p>5.</p> <p>8, 15 and 16</p> <p>OR 9, 13 and 17</p> <p>OR 10, 11 and 18</p>	<p>B2</p>	<p>$3 \times n + 1 = 3n + 1$ is B1 – 1 = B0.</p> <p>All three numbers must be less than 25.</p> <p>B1 for three numbers with a range of 8.</p> <p>B1 for three numbers whose total = 39.</p>
--	-----------	---

16.	8, 15 and 16	B2	All three numbers must be less than 25.
OR	9, 13 and 17		B1 for three numbers with a range of 8.
OR	10, 11 and 18		B1 for three numbers with a total = 39.

4.(a) (i) 22 (cm)	B1	
4.(a) (ii) 18 cm ²	B1 U1	
4.(b) Rectangle 3 × 6	B1	Accept any rectangle with an area of 18 cm ² which fits on the grid e.g. 4 × 4.5 FT 'their (a)(ii)'

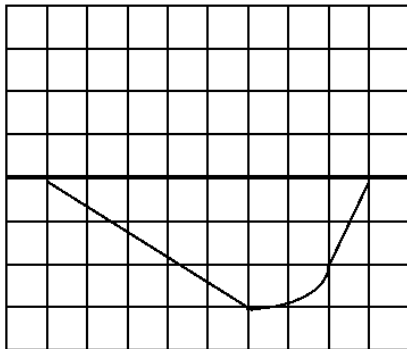
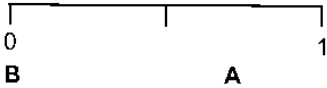
3.(a) Sum of numbers (225)	M1	Allow for an unsupported value between 192 and 258 inclusive.
Sum of numbers / 9 25	m1 A1	Award this m 1 for 'their sum' + 9 CAO
3.(b) Correct explanation e.g. Neil hasn't written the numbers in (ascending or descending) order.	E1	

4.	3 AND 11	B2	Mark final answer. Accept in any order. B1 for two numbers with a sum of 14 OR B1 for two numbers with a range of 8.
----	----------	----	---

<p>10.(a) 1, 4 and 25</p>	<p>B3</p>	<p>Answer space takes precedence. Accept 1², 2² and 5². B2 for writing three numbers which add to 30, two of which are square (e.g. 16, 9, 5). B1 for writing three numbers: <ul style="list-style-type: none"> at least two of which are square, OR which add to 30, one of which is square, OR which are all square. SC2 for an answer of 1, 2 and 5 with correct working. SC1 for an unsupported answer of 1, 2 and 5</p>
<p>10.(b) 1, 5, 7, 7 OR 3, 5, 7, 7</p>	<p>B3</p>	<p>Answer space takes precedence. B2 for writing four <u>odd and positive</u> numbers (not 7, 7, 7, 7) which fulfil one of the conditions: <ul style="list-style-type: none"> the mode of the numbers is 7 the median of the numbers is 6 OR for an answer which satisfies <u>both</u> conditions but includes an even number (e.g. 2, 5, 7, 7) B1 for writing four numbers which fulfil only one of the conditions: <ul style="list-style-type: none"> the mode of the numbers is 7 the median of the numbers is 6 OR for an answer of 7, 7, 7, 7.</p>
<p>11.(a) 0.125×1176 or equivalent. = 147 ISW</p>	<p>M1 A1</p>	
<p>11.(b) 4·7</p>	<p>B2</p>	<p>If further incorrect work shown e.g. '4·7 = 5' then allow B1 only. B1 for sight of 4·6 or 4·68(.....) or 4·70</p>
<p>12. $f = 73(^{\circ})$ $g = 128 - 73$ = 55(^{\circ})</p>	<p>B1 M1 A1</p>	<p>F.T. 128 - 'their f.'</p>
<p><i>Alternative method</i> $f = 73(^{\circ})$ $g = 180 - (180 - 128) - 73$ = 55(^{\circ})</p>	<p>B1 M1 A1</p>	<p>FT 'their f.'</p>
<p>13. $\begin{array}{r} (1) \ 5 \ (9) \\ (7) \ (8) \ 2 \\ \hline 9 \ (4) \ (1) \end{array}$</p>	<p>B3</p>	<p>B1 for each. No F.T.</p>
<p>14.(a) $\frac{1}{12}$</p>	<p>B1</p>	
<p>14.(b) D</p>	<p>B1</p>	
<p>14.(c) $\frac{1}{3}$</p>	<p>B1</p>	
<p>15. Sight of 6·25 (hrs) OR 375 (min) (Planning =) $\frac{2}{5} \times 6.25$ OR $\frac{2}{5} \times 375$ = 2·5 (hrs) OR 150 (min) (Remainder of work = 6·25 - 2·5 OR 375 - 150 =) 3·75 (hrs) OR 225 (min) = 3 hours 45 minutes</p>	<p>B1 M1 A1 B1 B1</p>	<p>F.T. 'their time' in hours or in minutes. May be seen in parts (1/5th and then 2/5ths) [Note: 2/5 × 6·15 OR 2/5 × 615 is B0M1(FT) = 2·46(hrs) OR 246(min) A1(FT) BUT A0 if 2·46 then used as 2h 46m] F.T. 'their derived times' using same units. F.T. correct conversion of 'their times', correct to the nearest minute (rounded or truncated), if of equivalent difficulty. Allow unambiguous indication of units.</p>

14.	3 AND 11	B2	Accept in any order. B1 for two numbers with a sum of 14 OR B1 for two numbers with a range of 8. Accept non-integers for B1 marks.
-----	----------	----	--

WJEC GCSE MATHEMATICS
AUTUMN 2021 MARK SCHEME

Unit 1: Foundation Tier	Mark	Comments
1.(a) Ninety-five thousand and forty-eight	B1	
1.(b) 931	B1	
1.(c) 1250	B1	
1.(d) 208	B1	
1.(e) 1,2,3,6,9,18	B2	B1 for 4 or 5 correct and 0 incorrect B1 for 5 or 6 correct and 1 incorrect Ignore repeated numbers Accept products 1×18 , 2×9 , 3×6
2.(a) 94 (mm)	B1	Accept 92 to 96 (mm)
2.(b) 136°	B1	Accept 134 to 138°
3.(a) 16	B1	
3.(b) $\frac{3}{4}$	B1	Mark final answer.
3.(c) 28	B1	
4. 	B2	B1 for correct longer straight line. B1 for correct curve AND shorter straight line. The lines must pass through the correct points.
5.(a) 4.3×1000 4300 (g)	M1 A1	
5.(b) $3 \times 100 \div 6$ 50 (cm)	M1 A1	If M0 A0, award SC1 for sight of 300(cm) or 0.5(m).
6. 	B1 B1	A should be between 0.6 and 0.8 B should be at 0

WJEC GCSE MATHEMATICS
AUTUMN 2021 MARK SCHEME

Unit 2: Foundation Tier	Mark	Comments																
1.(a) 5169	B1																	
1.(b) 6502	B1																	
1.(c) 186	B1																	
1.(d) 45	B1																	
2.(a) 5, 5, 5, 5	B1																	
2.(b) Exactly two 3s and any other two numbers	B1	Accept in any order.																
2.(c) Exactly one 2 and any other three numbers	B1	Accept in any order.																
3.(a) 40 065	B1																	
3.(b) 5400	B1																	
4.(a) rhombus	B1																	
4.(b) equilateral triangle	B1																	
5. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>71</td> <td>60</td> <td>78</td> <td>41</td> </tr> <tr> <td>26</td> <td>85</td> <td>27</td> <td>112</td> </tr> <tr> <td>95</td> <td>105</td> <td>42</td> <td>8</td> </tr> <tr> <td>58</td> <td>0</td> <td>103</td> <td>89</td> </tr> </table>	71	60	78	41	26	85	27	112	95	105	42	8	58	0	103	89	B3	B2 for 3 rows or 3 columns with a total of 250. B1 for 1 or 2 rows or 1 or 2 columns with a total of 250.
71	60	78	41															
26	85	27	112															
95	105	42	8															
58	0	103	89															
6.(a) 98	B1																	
6.(b) Subtract 13 (from the previous term)	B1	Accept -13, goes down in 13s, etc.																
6.(c) x-2 (years old)	B1	Mark final answer.																
7.(a) Sum of numbers (262) Sum of numbers $\div 4$ 65.5 or equivalent	M1 m1 A1	Allow for an unsupported value between 173 and 351. Award this m1 for 'their sum' $\div 4$ CAO. Allow 131/2. If no marks awarded, allow SC1 for (64 + 89 + 83 + 26 $\div 4$ =) 242.5 or equivalent.																
7.(b) (65.5 + 1 =) 66.5	B1	F.T. 'their mean' from (a). Allow 133/2.																
8.(a) 23.04	B1	Accept $23 \frac{1}{25}$ or equivalent e.g. 576/25																
8.(b) 7.9	B1	Accept $7 \frac{9}{10}$ or equivalent e.g. 79/10																
8.(c) 0.04×325 or equivalent = 13 ISW	M1 A1																	
9. (Oliver's number is) 90	B3	B2 for a final answer <u>between 40 and 95</u> satisfying 2 of the 3 conditions. (45, 54, 60, 72) B1 for a final answer <u>between 40 and 95</u> satisfying only 1 of the 3 conditions. (40, 42, 44, 46, 48, 50, 52, 56, 58, 62, 63, 64, 66, 68, 70, 74, 75, 76, 78, 80, 81, 82, 84, 86, 88, 92, 94)																
OC Organisation and Communication.	OC1	For OC1, candidates will be expected to: <ul style="list-style-type: none"> present their response in a structured way explain to the reader what they are doing at each step of their response lay out their explanation and working in a way that is clear and logical write a conclusion that draws together their results and explains what their answer means 																

<p>14. Sight of 9 AND 49 $n + 9 = 49$</p> <p style="text-align: center;">(n =) 40</p>	<p>B1 M1</p> <p>A1</p>	<p>Any unambiguous indication that this linear relationship is being considered (including 'trial and improvement'). FT their $\sqrt{81}$ ($\neq 81$) AND 7^2 ($\neq 7$) for M1 and possibly A1 if at least one correct value used. FT for M1 <u>only</u> if neither correct value used. Award M1 if $49 - 9$ seen. Mark final answer.</p>
<p>15. Indicates 2 (letters out of 6 gain points) (Expected number of wins =) $\frac{2}{6} \times 24$ or equivalent $= 8$ (Points gained =) 8×10 $= 80$ (points) AND 'No' (Leah is not expected score 100 points)</p>	<p>B1 M1</p> <p>A1 M1 A1</p>	<p>Any unambiguous indication. FT 'their stated number of '10 point' letters'. Award M1A1 for $8/24$ suggesting '8 wins out of 24' FT 'their derived 8×10 <u>only</u> if 'their derived $8 < 24$'. FT their <u>derived</u> number of points</p>
<p><u>Alternative method 1</u> Indicates 2 (letters out of 6 gain points) (Each letter expected to be drawn) $\frac{24}{6}$ (times) $= 4$ (times) (Points gained =) $4 \times 2 \times 10$ $= 80$ (points) AND 'No' (Leah is not expected score 100 points)</p>	<p>B1 M1</p> <p>A1 M1 A1</p>	<p>Any unambiguous indication. FT 'their derived 4' and 'their stated 2'. FT their <u>derived</u> number of points.</p>
<p><u>Alternative method 2</u> Indicates 2 (letters out of 6 gain points) (Expected number of wins =) $\frac{2}{6} \times 24$ or equivalent $= 8$ (Number of wins required =) $\frac{100}{10}$ $= 10$ (wins) AND 'No' (Leah is not expected score 100 points)</p>	<p>B1 M1</p> <p>A1 M1 A1</p>	<p>Any unambiguous indication. FT 'their stated number of '10 point' letters'. Award M1A1 for $8/24$ suggesting '8 wins out of 24' FT their <u>derived</u> number of <u>expected</u> wins. <u>Note for Alternative method 2</u> If 'number of wins required' is calculated before calculating 'number of expected wins' then the conclusion ('AND') will be attached to the 8 rather than the 10.</p>
<p>16. $4x + 5 = 57$ or equivalent $4x = 52$ $x = 13$</p>	<p>M1 A1 A1</p>	<p>FT from $4x = k$. Accept $x = k/4$ (but, if on FT k is a multiple of 4, final answer must be given as a whole number.) M1A1A0 for '$x = 52/4$' Mark final answer. Allow (M1)A1A1 for a correct embedded answer BUT only (M1)A1A0 if contradicted by $x \neq 13$.</p>
<p>17. 3, 4, 4, 9 OR 3, 3, 5, 9.</p>	<p>B3</p>	<p>B1 for a range = 6. B1 for a total = 20. B1 for a median = 4. Penalise use of negative or non-integer values -1. FOUR numbers must be shown, otherwise B0.</p>
<p>18. Use of Distance / Time $\frac{100}{2.5}$ or equivalent $= 40$ (mph)</p>	<p>M1 M1</p> <p>A1</p>	<p>Allow M1 even for e.g. $100 / 2.3(0)$ or $100/150$. C.A.O.</p>

9. 7, 7, 10, 12 (in any order)	B3	<p><i>Numbers shown <u>in</u> number boxes take precedence.</i></p> <p>The four conditions:</p> <ul style="list-style-type: none">• All numbers between 1 and 15 inclusive.• Unique mode = 7.• Median = 8.5.• Total = 36. <p>B2 for three conditions met. B1 for two conditions met.</p> <p>FOUR numbers must be shown, otherwise B0. Award B1 only for 7, 7,10,10 OR 7, 7,11,11 (not a unique mode).</p>
---------------------------------------	----	---

<p>5(a)</p> <p>(Tax at 22%) 0.22×15000 or $0.22 \times (25000 - 10000)$ or equivalent</p> <p>(Tax at 35%) 0.35×3000 or $0.35 \times (28000 - 25000)$ or equivalent</p> <p>(Total tax due $3300 + 1050 =$ 4350 (euros)</p> <p>(Tax still owed $4350 - 3600 =$) 750 (euros)</p>	<p>M2</p> <p>M2</p> <p>A2</p> <p>B1</p>	<p>Ignore £ for € throughout M1 for appropriate sight of $25000 - 10000 (= €15000)$</p> <p>M1 for $28000 - 25000 (= €3000)$</p> <p>CAO A1 for sight of 3300 (euros) or 1050 (euros)</p> <p>FT for positive answers only, 'their derived $4350' - 3600$, provided $3300 + \dots$ or $\dots + 1050$ seen, i.e. sum of two amounts with at least one amount correct</p> <p><u>If no marks, for special cases award one of the following:</u></p> <table border="1" data-bbox="852 667 1422 913"> <tr> <td data-bbox="852 667 1289 801"> $(0.22 \times (28000 - 3600 - 10000) =)$ $(0.22 \times (24400 - 10000) =)$ $(0.22 \times 14400 =)$ <p style="text-align: right;">(€) 3168</p> </td> <td data-bbox="1289 667 1422 801"> <p>SC2</p> </td> </tr> <tr> <td data-bbox="852 801 1289 913"> $0.22 \times (28000 - 3600 - 10000)$ or $0.22 \times (24400 - 10000)$ or 0.22×14400 </td> <td data-bbox="1289 801 1422 913"> <p>SC1</p> </td> </tr> </table>	$(0.22 \times (28000 - 3600 - 10000) =)$ $(0.22 \times (24400 - 10000) =)$ $(0.22 \times 14400 =)$ <p style="text-align: right;">(€) 3168</p>	<p>SC2</p>	$0.22 \times (28000 - 3600 - 10000)$ or $0.22 \times (24400 - 10000)$ or 0.22×14400	<p>SC1</p>
$(0.22 \times (28000 - 3600 - 10000) =)$ $(0.22 \times (24400 - 10000) =)$ $(0.22 \times 14400 =)$ <p style="text-align: right;">(€) 3168</p>	<p>SC2</p>					
$0.22 \times (28000 - 3600 - 10000)$ or $0.22 \times (24400 - 10000)$ or 0.22×14400	<p>SC1</p>					
<p>5(b) $3600 \div 1.11$</p> <p style="text-align: right;">(£) 3243.24</p>	<p>M1</p> <p>A1</p>	<p>Answer space takes precedence Sight of (£) 3243 or 3243.2(4324....) implies M1</p>				

8. (value of 6 th number =) $6 \times 8.5 - 5 \times 7$ $= (51 - 35)$	M2	Award M1 for sight of any one of the following: <ul style="list-style-type: none">• 5×7• 35• 6×8.5• 51.
---	----	--

18. (value of 6 th number =) $6 \times 8.5 - 5 \times 7$ $= (51 - 35)$ $(=) 16$	M2 A1	Award M1 for sight of any one of the following <ul style="list-style-type: none"> • 5×7 • 35 • 6×8.5 • 51 CAO
19. (1 share =) $(\pounds)16.80 \div 8$ or equivalent (1 share =) $(\pounds)2.1(0)$ or equivalent (Total =) $(\pounds)18.9(0)$ or equivalent	M1 A1 A1	<i>Allow answers in pounds or pence.</i> Award M1 A1 for sight of $(\pounds)2.1(0) : (\pounds)16.80$. If M1 A0, then FT 'their $(\pounds)2.1(0) \times 9$ OR 'their $(\pounds)2.1(0) + (\pounds)16.8(0)$ If units given, then they must be correct e.g. award A1 for 1890 or 1890p but A0 for $\pounds 1890$
<i>Alternative method:</i>		

<p>5.</p> <p>$2(n-7)$ or equivalent e.g. $2n-14$.</p>	<p>B3</p>	<p>Answer space takes precedence.</p> <p>For B3, accept as a final answer of:</p> <ul style="list-style-type: none"> • $2 \times (n-7)$ • $(n-7)2$ • $(n-7) \times 2$. <p>Award B2 if incorrect subsequent working for one of the above.</p> <p>Award B2 for sight of one of the following:</p> <table border="1" data-bbox="852 495 1310 842"> <thead> <tr> <th>missing brackets</th> <th>error in Samir's age</th> </tr> </thead> <tbody> <tr> <td>• $2 \times n-7$</td> <td>• $2(n+7)$</td> </tr> <tr> <td>• $n-7 \times 2$</td> <td>• $2 \times (n+7)$</td> </tr> <tr> <td></td> <td>• $(n+7)2$</td> </tr> <tr> <td></td> <td>• $(n+7) \times 2$</td> </tr> <tr> <td></td> <td>• $2(7-n)$</td> </tr> <tr> <td></td> <td>• $2 \times (7-n)$</td> </tr> <tr> <td></td> <td>• $(7-n)2$</td> </tr> <tr> <td></td> <td>• $(7-n) \times 2$</td> </tr> <tr> <td></td> <td>• $2n+14$</td> </tr> <tr> <td></td> <td>• $14-2n$</td> </tr> </tbody> </table> <p>Award B1 for sight of one of the following:</p> <ul style="list-style-type: none"> • $n-7$ • $2 \times n+7$ • $n+7 \times 2$ • $2 \times 7-n$ • $7-n \times 2$ • $2n-7$ • $n-14$ • $n-72$. <p>Allow use of a different letter for n.</p>	missing brackets	error in Samir's age	• $2 \times n-7$	• $2(n+7)$	• $n-7 \times 2$	• $2 \times (n+7)$		• $(n+7)2$		• $(n+7) \times 2$		• $2(7-n)$		• $2 \times (7-n)$		• $(7-n)2$		• $(7-n) \times 2$		• $2n+14$		• $14-2n$
missing brackets	error in Samir's age																							
• $2 \times n-7$	• $2(n+7)$																							
• $n-7 \times 2$	• $2 \times (n+7)$																							
	• $(n+7)2$																							
	• $(n+7) \times 2$																							
	• $2(7-n)$																							
	• $2 \times (7-n)$																							
	• $(7-n)2$																							
	• $(7-n) \times 2$																							
	• $2n+14$																							
	• $14-2n$																							

4.(c) parallelogram	B1	
5. 11 13 15 17 20 22 29 or 29 22 20 17 15 13 11	M1	For arranging the 7 numbers in ascending or descending order

16.(a)	28	B1	Allow B1 for a correct embedded answer (e.g. $28 \div 4 = 7$ BUT B0 if contradicted by total $\neq 28$). Allow the sequence 7,14,21,28 for B1, but only if no further numbers are shown.
--------	----	----	---

16.(b)

Four numbers (in any order) with a total of 28 and range of 6
e.g.

3	7	9	9
3	8	8	9
4	7	7	10
4	6	8	10
4	5	9	10
4	4	10	10
5	5	7	11
5	6	6	11

B2

Numbers may be seen in any order.
Accept answers using fractions and decimals.
FT 'their total' from 16(a).

Award B1 for **four** numbers with one of the following:

- total = 28
- total = 'their total' from 16(a)
- range = 6.

<p>5.(a) 36</p>	B1	<p>Allow B1 for a correct embedded answer (e.g. $36 \div 4 = 9$ BUT B0 if contradicted by total $\neq 36$).</p> <p>Allow the sequence 9, 18, 27, 36 for B1, but only if no further numbers are shown.</p>																								
<p>5.(b) Four numbers including 11, 11 AND a pair of non-identical numbers whose sum is 14</p> <table border="1" data-bbox="331 398 587 593"> <tr><td>1</td><td>13</td><td>11</td><td>11</td></tr> <tr><td>2</td><td>12</td><td>11</td><td>11</td></tr> <tr><td>3</td><td>11</td><td>11</td><td>11</td></tr> <tr><td>4</td><td>10</td><td>11</td><td>11</td></tr> <tr><td>5</td><td>9</td><td>11</td><td>11</td></tr> <tr><td>6</td><td>8</td><td>11</td><td>11</td></tr> </table>	1	13	11	11	2	12	11	11	3	11	11	11	4	10	11	11	5	9	11	11	6	8	11	11	B2	<p>Numbers may be seen in any order. Accept answers using fractions, decimals or negative numbers.</p> <p>FT 11, 11 AND two numbers whose sum is 'their total' from (a) – 22 for a possible B2 or B1.</p> <p>Award B1 for four numbers with one of the following:</p> <ul style="list-style-type: none"> • total = 36 • total = 'their total' from 5(a) • four numbers with a unique mode of 11 (11, 11, ?, ? or 11, 11, 11, ? or 11, 11, 11, 11) • 7, 7, 11, 11.
1	13	11	11																							
2	12	11	11																							
3	11	11	11																							
4	10	11	11																							
5	9	11	11																							
6	8	11	11																							

point C.		
5.(a) 3	B1	
5. (b) 4	B2	B1 for 1 2 3 4 8 8 9 (ascending or descending list)
5.(c) (Missing value =) $5 \times 3 - (7 + 2)$	M2	Award M2 for sight of unambiguous $15 - 9$ Award M1 for sight of (Total of all 3 values =) 5×3 or unambiguous '15'
(Missing value = $15 - 9 =$) 6	A1	CAO
<u>5.(c) Alternative method (trial and improvement)</u>		
A trial of any value	M1	<u>'Their value' + 7 + 2</u> evaluated correctly 3
An improved trial	m1	An improved trial means that their choice of value takes them in the right direction.
6	A1	May be seen as an embedded answer, unless contradicted. If contradicted award M1 m1 A0. Award M1 m1 A1 for a correct answer of 6.

<p>6(a)(i) Unambiguously indicates or states 'Yes' with a reason, e.g. 'both 25 kg to 35 kg', 'the highest frequencies at the same mass'</p>	E1	<p><i>Ignore any additional spurious or contradictory statements provided 'Yes' selected</i></p> <p>Allow 'Yes' with a reason, e.g. 'both at 30 kg', 'both at the same mass', 'both have the same mass', 'tallest (highest frequency) is 30kg for both polygons'</p> <p>Do not accept 'Yes' with a reason, e.g. 'don't know', 'both in the same place', 'the groups have the same width', 'the graph tells us this'</p>
<p>6(a)(ii) Unambiguously indicates or states 'Can't tell' with a reason, e.g. 'there were 30 dogs with a masses between 15kg and 25kg', 'no raw data is given', 'the actual mass of each dog is not given', 'the data is grouped'</p>	E1	<p><i>Ignore any additional spurious or contradictory statements provided 'Can't tell' selected</i></p> <p>Allow 'Can't tell' with a reason, e.g. 'doesn't show this', 'you can't tell the exact number of dogs' 'doesn't give the amount of dogs'</p> <p>Do not accept 'Can't tell' with a reason, e.g. 'don't know', 'it is an estimate', 'it isn't accurate', 'because they can be anywhere from 10kg to 20kg'</p>
<p>6(a)(iii) Unambiguously indicates or states 'Correct' with a reason, e.g. 'Pencwm polygon shows a greater drop for greater masses', 'fewer dogs but more large dogs in Glanafon', 'more dogs in Pencwm, but fewer large dogs', 'about the same number of large dogs, with fewer dogs in Glanafon', 'about the same number of large dogs, with more dogs in Pencwm',</p>	E1	<p><i>Ignore any additional spurious or contradictory statements provided 'Correct' selected</i></p> <p>Do not allow a reason based on calculations of proportions alone, e.g. Pencwm 27.5%, Glanafon 41.6%</p> <p>Allow 'Correct' with a reason, e.g. 'Pencwm (polygon) shows a steeper drop from 30 kg', 'line for Pencwm is steeper (drop)', 'Glanafon (polygon) has a less steep drop for larger dogs', 'the greater masses are more frequent (in Glanafon)', '2 of the 3 points for Glanafon are above Pencwm', 'Pencwm line drops below Glanafon after 40 (kg)'</p> <p>Do not accept 'Correct' with a reason, e.g. '36 dogs in Pencwm and 37 dogs in Glanafon' alone without considering proportion, 'the greatest is 45 kg', 'higher frequency in Glanafon', 'Pencwm is bigger but doesn't have higher proportion' 'as seen by the skew in (the) Glanafon (polygon)', 'seen by the shape (of the polygon) for Glanafon'</p>

<p>6(b) (Total number of dogs $20 + 30 + 45 + 25 + 7 + 4 =$ 131</p> <p>$10 \times 20 + 20 \times 30 + 30 \times 45 + 40 \times 25 + 50 \times 7 + 60 \times 4$ $(= 200 + 600 + 1350 + 1000 + 350 + 240)$ $(= 3740)$</p> <p style="text-align: right;">$+ 131$</p> <p>(28.5(496.... kg) so) 3.95 (kg) (less)</p>	<p>B1 May be implied by the sight of $((20 + 30 + 45 + 25 + 7 + 4) \div 6 =) 21.8(33\dots)$</p> <p>M1 Ignore any additional products seen FT 'their midpoints' provided at least 5 are within or at the bounds of the relevant groups e.g. use of</p> <ul style="list-style-type: none"> • lower bounds of each group gives 3085 • upper bounds of each group gives 4395 <p>m1 FT an error in summing 20, 30, 45, 25, 7 and 4</p> <p>A2 CAO ISW further rounding or truncation Allow 4 (kg) from correct working Accept (29 (kg) and) 3.5 (kg) from correct working</p> <p>Award A1 for any of the following as the final answer</p> <ul style="list-style-type: none"> • 28.5(496.... kg) • 29 (kg) (from correct working) <p>OR</p> <p>Award A1 on FT from M1 m1 previously awarded for a correct evaluation of 'their estimate mean' e.g. use of lower bounds gives $(3085/131 =) 23.54\dots$</p>
<p><u>6(b) Alternative MS if Glanafon's last 2 points used for possible award of B1 M1 m1 only</u> (Sight of $20 + 30 + 45 + 25 + 10 + 7 =$) 137</p> <p>$10 \times 20 + 20 \times 30 + 30 \times 45 + 40 \times 25 + 50 \times 10 + 60 \times 7$ $(= 200 + 600 + 1350 + 1000 + 500 + 420)$ $(= 4070)$</p> <p style="text-align: right;">$+ 137$</p>	<p>B1 May be implied by the sight of $((20 + 30 + 45 + 25 + 10 + 7) \div 6 =) 22.8(33\dots)$</p> <p>M1 Ignore any additional products seen FT 'their midpoints' provided at least 5 are within or at the bounds of the relevant groups e.g. use of</p> <ul style="list-style-type: none"> • lower bounds of each group gives 3385 • upper bounds of each group gives 4755 <p>m1 FT an error in summing 20, 30, 45, 25, 10 and 7</p>

<p>7(a) $5 \times 42 - (40 + 37 + 39 + 48)$ or $210 - 164$ or equivalent OR $40 + 37 + 39 + 48 + \dots = 5 \times 42$ or $164 + \dots = 210$</p> <p style="text-align: right;">(Friday) 46 (mm)</p>	<p>M2</p> <p>A1</p>	<p>May be shown in stages Allow missing brackets as the intention to subtract</p> <p>M1 for sight of any one of the following:</p> <ul style="list-style-type: none"> • 5×42 or 210 (mm) • the idea that $(40 + 37 + 39 + 48 + x) \div 5 = 42$, where x may be a gap, variable or a trial <p>CAO. Do not award from incorrect working Answer space takes precedence Do not allow an embedded answer</p>
<p>7(a) <u>Alternative methods</u> (Difference from mean) $42 + 2 + 5 + 3 - 6$ OR (Contributions to the mean each day) $5 \times (42 - \frac{40}{5} - \frac{37}{5} - \frac{39}{5} - \frac{48}{5})$ or equivalent (= 5×9.2)</p> <p style="text-align: right;">(Friday) 46 (mm)</p>	<p>M2</p> <p>A1</p>	<p>M1 for $42 - \frac{40}{5} - \frac{37}{5} - \frac{39}{5} - \frac{48}{5}$</p> <p>CAO. Answer space takes precedence</p>

$$7(b) \ 5 \times 42 \div 7 \quad \text{or} \quad 210 \div 7$$

30 (mm)

M1	Allow 'their 46' from (a) has been truncated or rounded, FT any of the following: <ul style="list-style-type: none">• 'their $5 \times 42 \div 7$• ('their $40 + 37 + 39 + 48$' + 'their 46') $\div 7$• $(164 + \text{'their 46'}) \div 7$
A1	Answer space takes precedence On FT, accept rounded or truncated answers provided working is shown

<p>9. (Amount of tea in full cup =)</p> $(44 \div 2) \times 7 \text{ or equivalent}$ $= 154 \text{ (ml)}$	<p>M1</p> <p>A1</p>	<p>M1 for full complete method. May be seen in stages.</p> <p>If M0 awarded, award SC1 for one of the following:</p> <ul style="list-style-type: none"> • appropriate sight of 22 • final answer of 61.6(ml) (from $(44 \div 5) \times 7$).
<p>9. <u>Alternative method</u></p> <p>(Amount of tea in full cup =)</p> $(44 \div 2) \times 5 + 44$ $= 154 \text{ (ml)}$	<p>M1</p> <p>A1</p>	<p>M1 for full complete method. May be seen in stages.</p> <p>If M0 awarded, award SC1 for appropriate sight of 22.</p>

9. $2500 \times (1 - 0.23) \times (1 - 0.04)^{39} \times (1 + 0.14)^{10}$ or $2500 \times 0.77 \times 0.96^{39} \times 1.14^{10}$ or equivalent	M3	May be seen in stages M2 for a product with any 3 correct terms OR M1 for a product with any 2 correct terms
(£) 1452(.30)	A1	CAO, ignore premature rounding in working provided answer is (£) 1452.(...), allow rounded to (£)1450 from correct working

15.(a) 36	B1	<p>Allow B1 for a correct embedded answer (e.g. $36 \div 4 = 9$ BUT B0 if contradicted by total $\neq 36$).</p> <p>Allow the sequence 9, 18, 27, 36 for B1, but only if no further numbers are shown.</p>																								
<p>15.(b) Four numbers including 11, 11 AND a pair of non-identical numbers whose sum is 14</p> <table border="1" data-bbox="331 398 587 593"> <tr><td>1</td><td>13</td><td>11</td><td>11</td></tr> <tr><td>2</td><td>12</td><td>11</td><td>11</td></tr> <tr><td>3</td><td>11</td><td>11</td><td>11</td></tr> <tr><td>4</td><td>10</td><td>11</td><td>11</td></tr> <tr><td>5</td><td>9</td><td>11</td><td>11</td></tr> <tr><td>6</td><td>8</td><td>11</td><td>11</td></tr> </table>	1	13	11	11	2	12	11	11	3	11	11	11	4	10	11	11	5	9	11	11	6	8	11	11	B2	<p>Numbers may be seen in any order. Accept answers using fractions, decimals or negative numbers.</p> <p>FT 11, 11 AND two numbers whose sum is 'their total' from (a) – 22 for a possible B2 or B1.</p> <p>Award B1 for four numbers with one of the following:</p> <ul style="list-style-type: none"> • total = 36 • total = 'their total' from 5(a) • four numbers with a unique mode of 11 (11, 11, ?, ? or 11, 11, 11, ? or 11, 11, 11, 11) • 7, 7, 11, 11.
1	13	11	11																							
2	12	11	11																							
3	11	11	11																							
4	10	11	11																							
5	9	11	11																							
6	8	11	11																							

Unit 2: Foundation Tier	Mark	Comments
7.(a) A correct explanation, e.g. <ul style="list-style-type: none"> • 'She hasn't used BIDMAS/ BODMAS/ Order of Operations'. • 'You must multiply before you add' • 'She should have multiplied first' • 'She has added the 10 and the 4 <u>first</u>, then multiplied by 9' 	E1	Accept ' $10 + 36 = 46$ '. Award E0 for: <ul style="list-style-type: none"> • an unsupported 46. • '$10 + 4 \times 9 = 46$'. • 'she added 10 and 4 together' • a correct explanation given but later contradicted • a correct explanation given with an incorrect answer to the calculation
7.(b) A correct explanation, e.g. <ul style="list-style-type: none"> • 'He has divided by 2 not divided by a half.' • 'He has worked out a half of 20 (not divided 20 by a half)'. • 'He should have multiplied by 2'. • 'He should have multiplied not divided'. • 'He should have divided by a half (not by 2)' 	E1	Accept ' $20 \div \frac{1}{2} = 40$ ' or ' $20 \times 2 = 40$ '. Award E0 for: <ul style="list-style-type: none"> • a correct explanation given but later contradicted • an unsupported 40 • 'he shouldn't have divided by 2' • 'there are more than 10 halves in 20' • a correct explanation given with an incorrect answer to the calculation
7.(c) A correct explanation, e.g. <ul style="list-style-type: none"> • 'She hasn't calculated the difference between the biggest number and the smallest number'. • 'She should have done $20 - 1$' 	E1	Accept ' $20 - 1 = 19$ '. Allow: <ul style="list-style-type: none"> • 'range = largest – smallest' • 'she didn't put the numbers in order first (before finding the difference between the end numbers)' • '11 isn't the biggest number <u>and</u> 7 isn't the smallest number' Award E0 for: <ul style="list-style-type: none"> • an unsupported 19 • $1 - 20$ (unless $= 19$ also seen) • '11 isn't the biggest number' • '7 isn't the smallest number' • 'smallest take away the biggest' • a correct explanation given but later contradicted. • a correct explanation given with an incorrect answer to the calculation
7.(d) A correct explanation, e.g. <ul style="list-style-type: none"> • 'They should halve ($\frac{1}{5}$ of the number to work out $\frac{1}{10}$ of the number)'. • 'They should divide by 2'. • 'They should multiply by 5 then divide by 10' 	E1	Accept equivalent explanations.

Unit 2: Intermediate tier	Mark	Comments
<p>7(a) <u>Method not directly working with a stated or omitted number of hours difference</u></p> <p>$0.324 \times 8 \times (10 \text{ or } 12) \times 7 \times 80 \div 1000$</p> <p>$0.324 \times 8 \times (12 \text{ or } 10) \times 7 \times 80 \div 1000$ with the intention to subtract</p> <p>(Saving is 17.418... – 14.515...=) (£) 2.90</p>	<p>M3</p> <p>m1</p> <p>A1</p>	<p>Methods may be shown in stages or be embedded <u>Use this method if 2 separate numbers of hours are used, which may not be correct, i.e. ≠12 and ≠10, with or without indication of subtraction</u></p> <p>Penalise every additional spurious term by reducing the count of correct terms by 1*</p> <p>Allow '× 32.4' for '× 0.324' M2 for any 4 or 5 correct terms* M1 for any 3 correct terms*</p> <p>Must be an indication of the intention to subtract, in either order FT from 5 (or 6) consistent correct terms for use of</p> <ul style="list-style-type: none"> the other value 10 or 12 respectively 'their number of hours' are 13 and 11 (incorrect) <p>Award m0 if inconsistent, i.e. not an equal number of consistent correct terms* between the expressions. Mark 'their better stated calculation' first if both are given</p> <p>CAO All working must be checked, do not award 5 marks for £2.90 from incorrect working.</p>
<p><u>Alternative method:</u> <u>Method directly working with a stated or omitted number of hours difference</u></p> <p>$0.324 \times 8 \times 2 \times 7 \times 80 \div 1000$</p> <p>(Saving is) (£) 2.90</p>	<p>M4</p> <p>A1</p>	<p><u>Methods may be shown in stages or be embedded</u> <u>Use this method if a single number of hours is used, which may not be correct, i.e. ≠2, or if the number of hours is omitted</u></p> <p>Do not allow 2 hours as a correct term from incorrect working, e.g. 13 – 11 = 2</p> <p>Penalise every additional spurious term by reducing the count of correct terms by 1*</p> <p>Allow '× 32.4' for '× 0.324' M3 for any 5 correct terms* M2 for any 4 correct terms* M1 for any 3 correct terms*</p> <p>CAO All working must be checked, do not award 5 marks for £2.90 from incorrect working.</p>

Unit 2: Intermediate Tier	Mark	Comments
7(b) Height = $\tan 68^\circ \times 3.3$ or height = $\frac{\sin 68^\circ \times 3.3}{\sin(90 - 68)^\circ}$	M2	Or alternative correct full method, isolating height M1 for $\tan 68^\circ = \text{height} / 3.3$ or $\frac{\text{height}}{\sin 68^\circ} = \frac{3.3}{\sin(90 - 68)^\circ}$ or equivalent
8.167... (m) or 8.17 (m) or 8.2 (m)	A1	Allow 8(m), 8.1(m) 8.16(m) from correct working

Unit 1: Intermediate Tier	Mark	Comments
8(a)(i) $200 - 80$ or $90 + 30$ 120 (customers)	M1 A1	
8(a)(ii) 32 seconds	B1	
8(a)(iii) $\frac{200-170}{200}$ or $\frac{30}{200}$ or $\frac{15}{100}$ $\frac{3}{20}$	M1 A1	Award M1 for 0.15 or 15% Only ignore further working if written as 0.15 or 15% If no marks, award SC1 for an answer of $\frac{17}{20}$ (from 40 seconds or less)
8(b)(i) 36	B1	
8(b)(ii) $46 - 20$ 26	M1 A1	Allow $20 - 46$
8(c) 'No' unambiguously stated or implied AND a reason, e.g. 'upper quartile is higher this year' '75% reading higher this year' 'interval was 37 (or 38) to 50 seconds last year, this year it is 46 to 50 seconds'	E1	Do not ignore incorrect values for the upper quartiles given, E0 if 'upper quartile' or '75%' stated with incorrect upper quartile readings Allow 'No' with a reason, e.g. '(last year) 38, (this year) 46' '(last year) 37(...), (this year) 46' Do not accept, e.g. 'range greater this year' 'lower quartile is lower this year' 'median higher this year' 'customers still waiting at 50 seconds'

<p>18. $\frac{a+b}{2} = b - a$</p> $a + b = 2(b - a)$ $a + b = 2b - 2a \quad \text{or} \quad a + 2a = 2b - b \quad (= 3a = b)$	<p>B1</p> <p>B1</p> <p>B1</p>	<p>B1 if only $(x =) -8$ AND $(x =) 5$ seen. (B1)</p> <p>Award B0 for $a + b \div 2 = b - a$ unless brackets are implied in later correct workings.</p> <p>May be implied by correct further work (e.g. $a + b = 2b - 2a$).</p> <p>Award final B1 only from convincing work.</p> <p>If no marks, award SC1 for one of the following:</p> <ul style="list-style-type: none"> $a + b \div 2 = b - a$ $\frac{a+b}{2} = a - b$ sight of $\frac{a+b}{2}$ AND $b - a$ showing the result is true (mean = range) for a pair of values a and b (where $3a = b$) e.g. stating that $a = 3$ and $b = 9$ and that $(9 + 3) \div 2 = 6$ and $9 - 3 = 6$.
<p>18. <u>Alternative method:</u> Assuming $b = 3a$ (Mean =) $\frac{a + 3a}{2}$ $= 2a$ Range = $3a - a = 2a$</p>	<p>M1</p> <p>A1</p> <p>B1</p>	<p>Working must be shown.</p> <p>Working must be shown.</p>

<p>9.(a) A correct explanation, e.g.</p> <ul style="list-style-type: none"> • 'He didn't write the numbers in (ascending/ descending) order (before identifying the middle number)'. • 'The median is 11'. • '20 is the largest number'. 	<p>E1</p>	<ul style="list-style-type: none"> • sight of 152 (but not 152B) <p>Allow</p> <ul style="list-style-type: none"> • 'because it's 11' • '20 is not the middle number' • a demonstration of how to correctly calculate the median e.g. circling the middle number in an ordered list. <p>Do not accept '11' or 'the median is the middle'.</p> <p>Do not ignore contradictory or incorrect comments e.g. 'put them in order first. the median is 14'</p>
<p>9.(b)(i) Sum of numbers (339)</p> <p>Sum of numbers $\div 5$</p> <p>$67 \cdot 8$ or $\frac{339}{5}$ or equivalent</p>	<p>M1</p> <p>m1</p> <p>A1</p>	<p>Allow for an unsupported value between 250 and 428.</p> <p>Award this m1 for 'their sum' $\div 5$</p> <p>CAO.</p> <p>ISW for candidates who go on to round their answer to 68.</p> <p>Do not allow $339 \div 5$.</p> <p>If no marks, award either:</p> <ul style="list-style-type: none"> • SC2 for an unsupported answer of 68 • SC1 for $(59 + 89 + 77 + 31 + 83 \div 5 =) 272 \cdot 6$ or equivalent.
<p>9.(b)(ii) $(67 \cdot 8 - 3 =) 64 \cdot 8$ or $\frac{324}{5}$</p>	<p>B1</p>	<p>F.T. 'their mean' from (a).</p> <p>Do not allow $324 \div 5$.</p>

11(a) 76 (g)	B1	Answer space takes precedence
11(b) $3 \times 400 \times 25 \div 100$ or $\frac{3}{4} \times 400$ or equivalent 300 (little gulls)	M1 A1	If no marks, award SC1 for $(\frac{1}{4} \times 400 =) 100$ (gulls)
11(c) 25(%)	B1	Answer space takes precedence
11(d)(i) Slender(-billed gulls)	B1	
11(d)(ii) Lower quartile	B1	<u>Strictly depends on B1 previously awarded in (d)(i)</u>

<p>11.</p> <p>(Electricity cost is) $654 \times (\pounds)0.30$ $(\pounds)196.2(0)$ or $19620(p)$</p> <p>(Cost of electricity and standing charge is $\pounds 196.20 + 54 =$) $(\pounds) 250.2(0)$</p> <p>(Total bill including VAT) $1.05 \times 250.2(0)$ or $250.2(0) + 12.51$</p> <p style="text-align: right;">$(\pounds)262.71$</p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>tins with 3, or their area with $4.8(m^2)$ is given</p> <p><u>Incorrect unit of money is penalised -1 once only on the first occurrence, by withholding an A or B mark</u></p> <p>Accept $654 \times 30(p)$</p> <p>If units are given they must be correct</p> <p>Accept $\pounds 196.20p$</p> <p>FT provided 654 used in a calculation for 'their cost of electricity'</p> <p>Do not accept if embedded with an incorrect interpretation of the standing charge, e.g. $196.20 + 3 \times 54 = (\pounds)358.20$ is B0</p> <p>If previous M0 A0 B0 for $(654 \times (\pounds)0.30 \times 3 =) \pounds 588.60$ AND $(588.60 + 54 \times 3 = 588.60 + 162 =) \pounds 750.60$, award SC1 for this consistent misunderstanding and then FT</p> <p>FT from 'their derived total of electricity' + 'their standing charge', accept rounding or truncation to a penny</p> <p>Allow M1 A0 for $1.05 \times$ 'their total rounded or truncated to a whole pound'</p> <p>If M0 A0 for inclusive of VAT cost, allow SC1 for an answer of $(\pounds)262.70$, provided not from incorrect working (allow from $250.20 + 12.50$)</p> <p>If final B0 M0 A0, award SC1 for the correct evaluation of $1.05 \times$ 'their derived cost of electricity' having not considered and omitted the standing charge, or previously subtracted the standing charge from 'their cost of electricity'</p>
---	---	--

12.	<p>Five values that satisfy both conditions:</p> <ul style="list-style-type: none"> • Total = 22·5 • Unique mode = 3·5 	B3	<p>May be written in any order. Answer boxes take precedence. Award B2 for one of the following:</p> <ul style="list-style-type: none"> • 5 values that total 22·5 • sight of $5 \times 4\cdot5$ and 5 values with a unique mode of 3·5 • sight of 22·5 and 5 values with a unique mode of 3·5. <p>Award B1 for one of the following:</p> <ul style="list-style-type: none"> • sight of $5 \times 4\cdot5$ • sight of 22·5 • 5 values with a unique mode of 3·5. <p>If answer boxes are blank, the 5 values need to be clearly identified in the working space.</p>															
	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 10%; text-align: center;">3·5</td> <td style="width: 10%; text-align: center;">3·5</td> <td colspan="3" style="text-align: center;">3 different values that total 15·5</td> </tr> <tr> <td style="text-align: center;">3·5</td> <td style="text-align: center;">3·5</td> <td style="text-align: center;">3·5</td> <td colspan="2" style="text-align: center;">2 values that total 12</td> </tr> <tr> <td style="text-align: center;">3·5</td> <td style="text-align: center;">3·5</td> <td style="text-align: center;">3·5</td> <td style="text-align: center;">3·5</td> <td style="text-align: center;">8·5</td> </tr> </table>	3·5	3·5	3 different values that total 15·5			3·5	3·5	3·5	2 values that total 12		3·5	3·5	3·5	3·5	8·5		
3·5	3·5	3 different values that total 15·5																
3·5	3·5	3·5	2 values that total 12															
3·5	3·5	3·5	3·5	8·5														

End of solutions